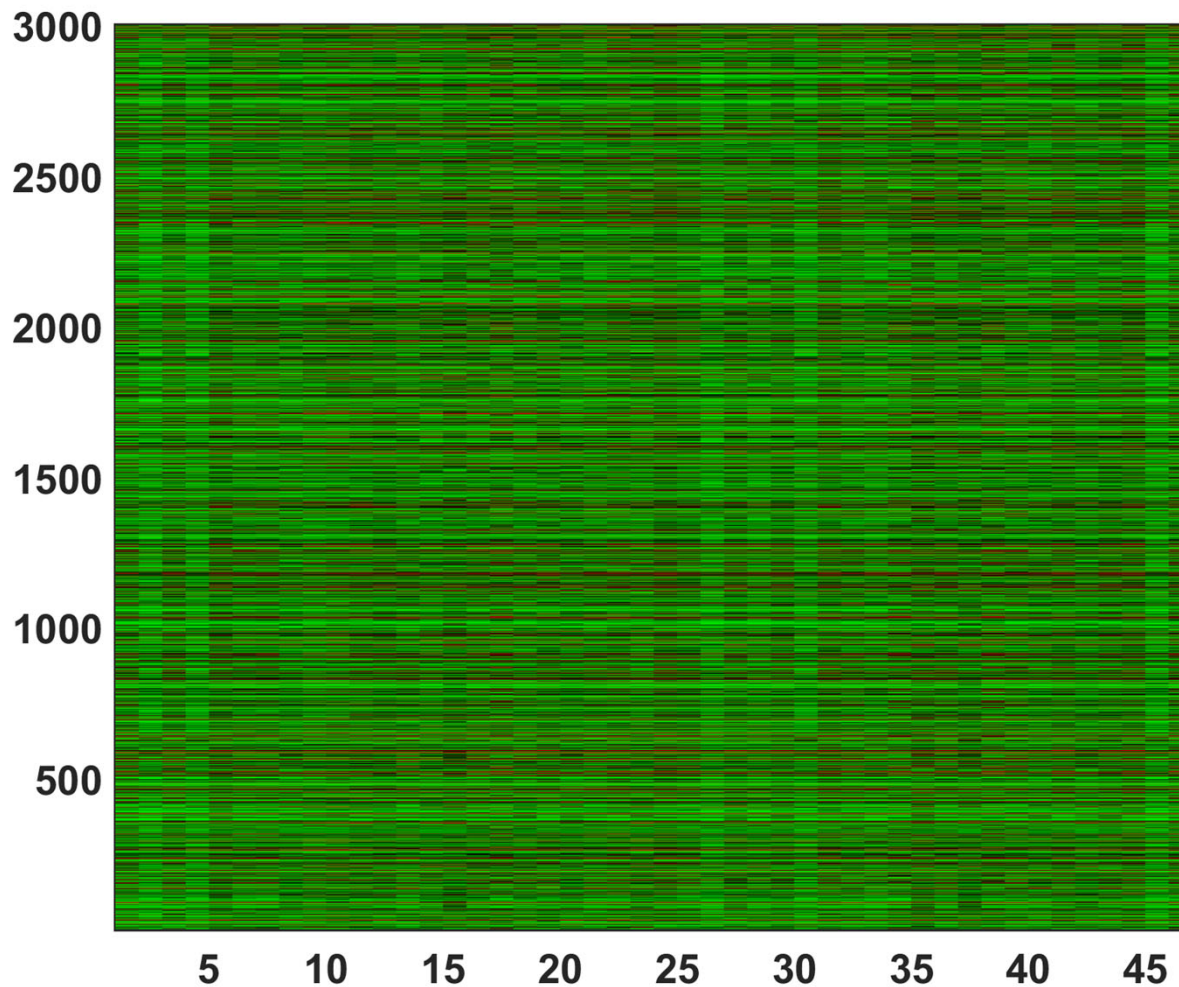


# Clustering and network analysis of gene expression data

Chapter 11 in  
Jonathan Pevsner,  
Bioinformatics and Functional Genomics,  
3<sup>rd</sup> edition  
(Chapter 9 in 2<sup>nd</sup> edition)

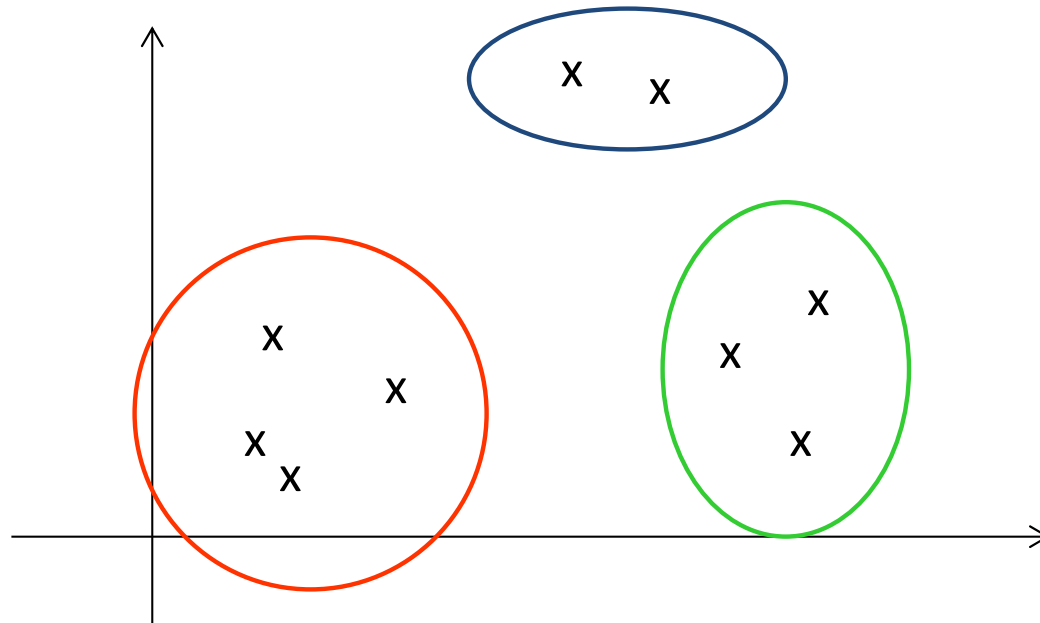
How to find the entire groups of mutually correlated genes if you have **many genes** and **many samples**?



Clustering to the rescue!

# What is clustering?

- The goal of **clustering** is to
  - group data points that are close (or **similar**) to each other
  - Usually, one needs to identify such groups (or clusters) in an **unsupervised** manner
  - Sometimes one takes into account **prior information** (Bayesian methods)
- Need to define some **distance  $d_{ij}$**  between **objects  $i$  and  $j$**
- Clustering is easy in **2 dimensions** but **hard in 3000 dimensions** -> need to somehow **reduce dimensionality**

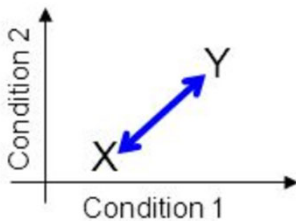


# How to define the distance?

- Euclidean distance:

- Most commonly used distance
- Sphere shaped cluster
- Corresponds to the geometric distance into the multidimensional space

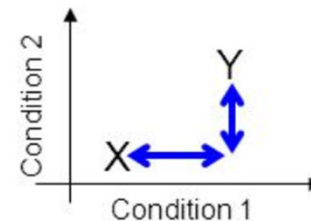
$$d(X, Y) = \sqrt{\sum_i (x_i - y_i)^2}$$



- City Block (Manhattan) distance:

- Sum of differences across dimensions
- Less sensitive to outliers
- Diamond shaped clusters

$$d(X, Y) = \sum_i |x_i - y_i|$$



The Canberra distance metric is calculated in R by

$$\sum \left( \frac{|x_i - y_i|}{|x_i + y_i|} \right).$$

Correlation coefficient distance

$$d(X, Y) = 1 - \rho(X, Y) = 1 - \frac{\text{Cov}(X, Y)}{\sqrt{\text{Var}(X) \cdot \text{Var}(Y)}}$$

# Common types of clustering algorithms

- Hierarchical if one doesn't know in advance the # of clusters
  - Agglomerative: start with N clusters and gradually merge them into 1 cluster
  - Divisive: start with 1 cluster and gradually break it up into N clusters
- Non-hierarchical algorithms
  - K-means clustering:
    - Iteratively apply the following two steps:
    - Calculate the centroid (center of mass) of each cluster
    - Assign each to the cluster to the nearest centroid
  - Principal Component Analysis (PCA)
    - plot pairs of top eigenvectors of the covariance matrix  $\text{Cov}(X_i, X_j)$  and uses visual information to group

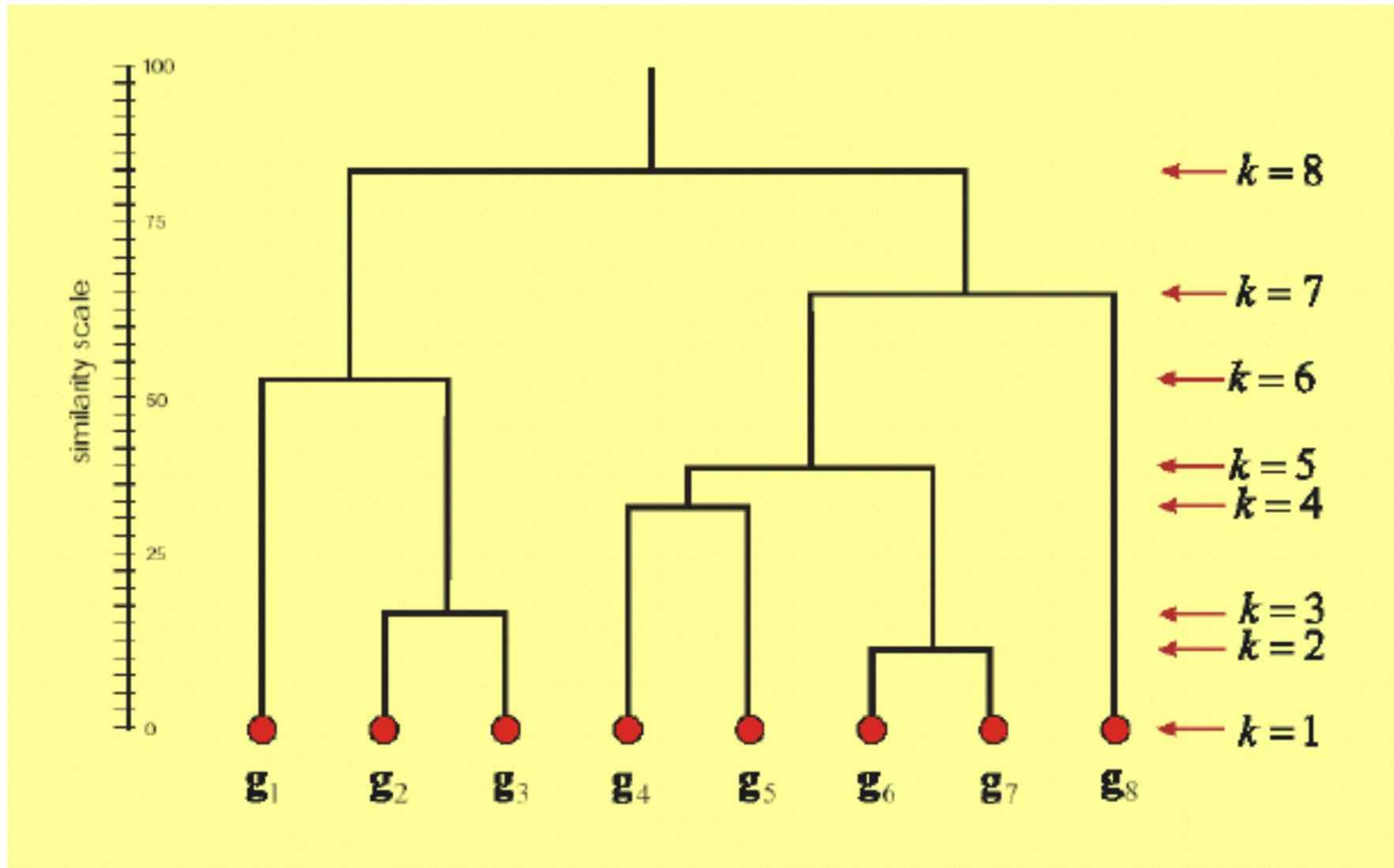
# Hierarchical clustering

# UPGMA algorithm

- Hierarchical agglomerative clustering algorithm
- **UPGMA** = **U**nweighted **P**air **G**roup **M**ethod with **A**rithmetic mean
- **Iterative** algorithm:
- Start with a **pair with the smallest  $d(X,Y)$**
- **Cluster these two together** and replace it with their arithmetic mean  $(X+Y)/2$
- **Recalculate all distances to this new “cluster node”**
- **Repeat** until all nodes are merged



# Output of UPGMA algorithm



# Clustering in Matlab

# Choices of distance metrics in `clustergram(... 'RowPDistValue' ...,` `'ColumnPDistValue' ...,)`

Metric	Description
'euclidean'	Euclidean distance (default).
'seuclidean'	Standardized Euclidean distance. Each coordinate difference between rows in X is scaled by dividing by the corresponding element of the standard deviation <code>S=nansd(X)</code> . To specify another value for S, use <code>D= pdist(X, 'seuclidean', S)</code> .
'cityblock'	City block metric.
'minkowski'	Minkowski distance. The default exponent is 2. To specify a different exponent, use <code>D = pdist(X, 'minkowski', P)</code> , where P is a scalar positive value of the exponent.
'chebychev'	Chebychev distance (maximum coordinate difference).
'mahalanobis'	Mahalanobis distance, using the sample covariance of X as computed by <code>nancov</code> . To compute the distance with a different covariance, use <code>D = pdist(X, 'mahalanobis', C)</code> , where the matrix C is symmetric and positive definite.
'cosine'	One minus the cosine of the included angle between points (treated as vectors).
'correlation'	One minus the sample correlation between points (treated as sequences of values).
'spearman'	One minus the sample Spearman's rank correlation between observations (treated as sequences of values).
'hamming'	Hamming distance, which is the percentage of coordinates that differ.
'jaccard'	One minus the Jaccard coefficient, which is the percentage of nonzero coordinates that differ.
custom distance function	A distance function specified using @: <code>D = pdist(X, @distfun)</code>  A distance function must be of form  <code>d2 = distfun(XI, XJ)</code>  taking as arguments a 1-by-n vector XI, corresponding to a single row of X, and an m2-by-n matrix XJ, corresponding to multiple rows of X. <code>distfun</code> must accept a matrix XJ with an arbitrary number of rows. <code>distfun</code> must return an m2-by-1 vector of distances d2, whose kth element is the distance between XI and XJ(k, :).

# Choices of hierarchical clustering algorithm in `clustergram( ...'linkage',...)`

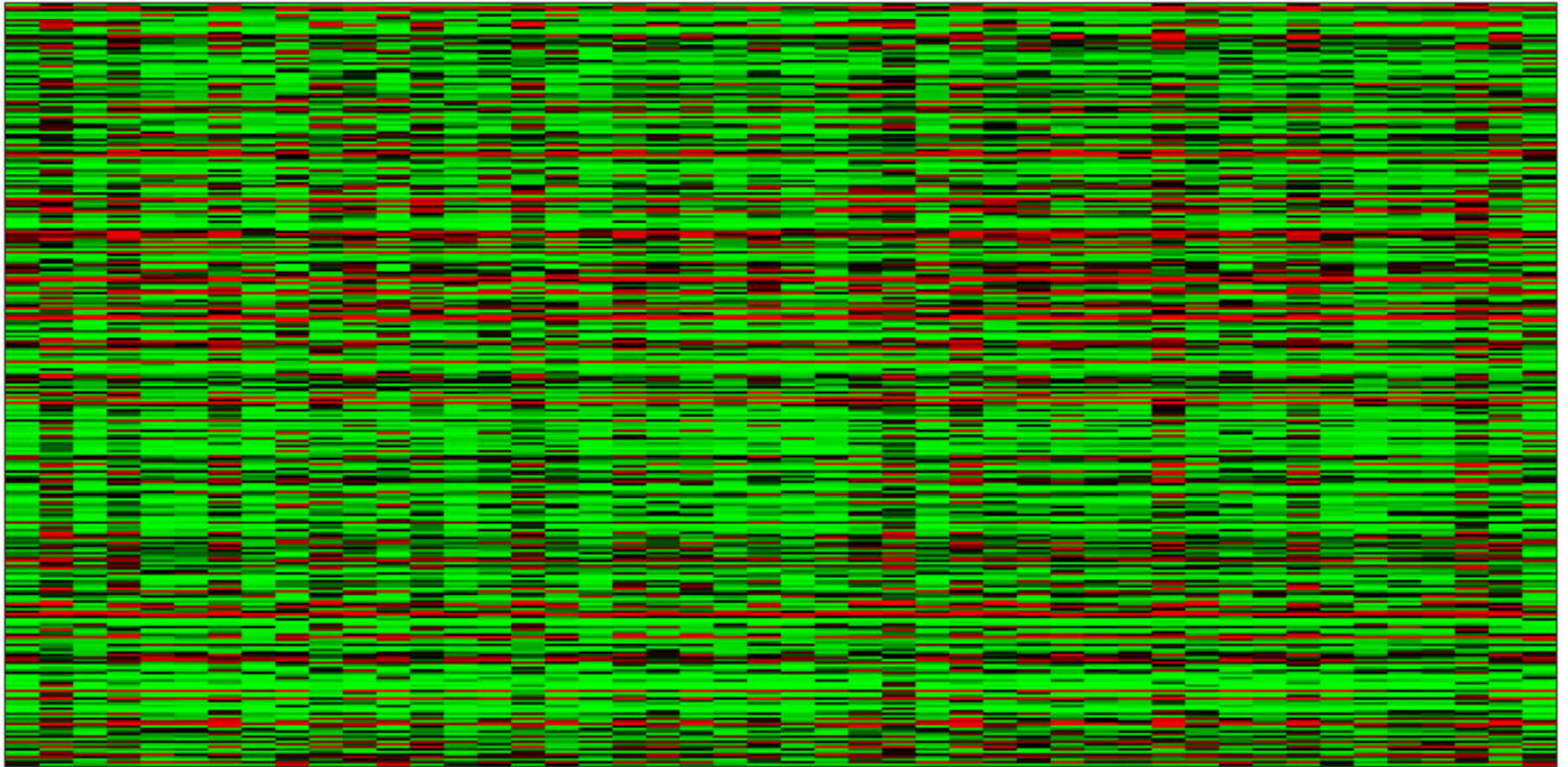
X	Matrix with two or more rows. The rows represent observations, the columns represent categories or dimensions.																
method	<p>Algorithm for computing distance between clusters.</p> <table border="1"><thead><tr><th>Method</th><th>Description</th></tr></thead><tbody><tr><td>'average'</td><td>Unweighted average distance (UPGMA)</td></tr><tr><td>'centroid'</td><td>Centroid distance (UPGMC), appropriate for Euclidean distances only</td></tr><tr><td>'complete'</td><td>Furthest distance</td></tr><tr><td>'median'</td><td>Weighted center of mass distance (WPGMC), appropriate for Euclidean distances only</td></tr><tr><td>'single'</td><td>Shortest distance</td></tr><tr><td>'ward'</td><td>Inner squared distance (minimum variance algorithm), appropriate for Euclidean distances only</td></tr><tr><td>'weighted'</td><td>Weighted average distance (WPGMA)</td></tr></tbody></table> <p><b>Default:</b> 'single'</p>	Method	Description	'average'	Unweighted average distance (UPGMA)	'centroid'	Centroid distance (UPGMC), appropriate for Euclidean distances only	'complete'	Furthest distance	'median'	Weighted center of mass distance (WPGMC), appropriate for Euclidean distances only	'single'	Shortest distance	'ward'	Inner squared distance (minimum variance algorithm), appropriate for Euclidean distances only	'weighted'	Weighted average distance (WPGMA)
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'weighted'	Weighted average distance (WPGMA)																

# Clustering group exercise

- Each group will analyze a **cluster of genes** identified in the T cell expression table
- Analyze the table of **top 100 genes by variance** in 47 samples
- Cluster them using:
  - Group 1: UPGMA = 'linkage', 'average', 'RowPDistValue', 'euclidean',
  - Group 2: 'linkage', 'single', 'RowPDistValue', 'cityblock',
  - Group 3: 'linkage', 'average', 'RowPDistValue', 'correlation',
  - Group 4: UPGMA = 'linkage', 'single', 'RowPDistValue', 'euclidean',
  - Group 5: UPGMA = 'linkage', 'weighted', 'RowPDistValue', 'correlation',
- Use `clustergram(..., 'Standardize','Row', 'linkage', as specified for your group, 'RowPDistValue' as specified for your group, 'RowLabels',gene_names1,'ColumnLabels', array_names)`

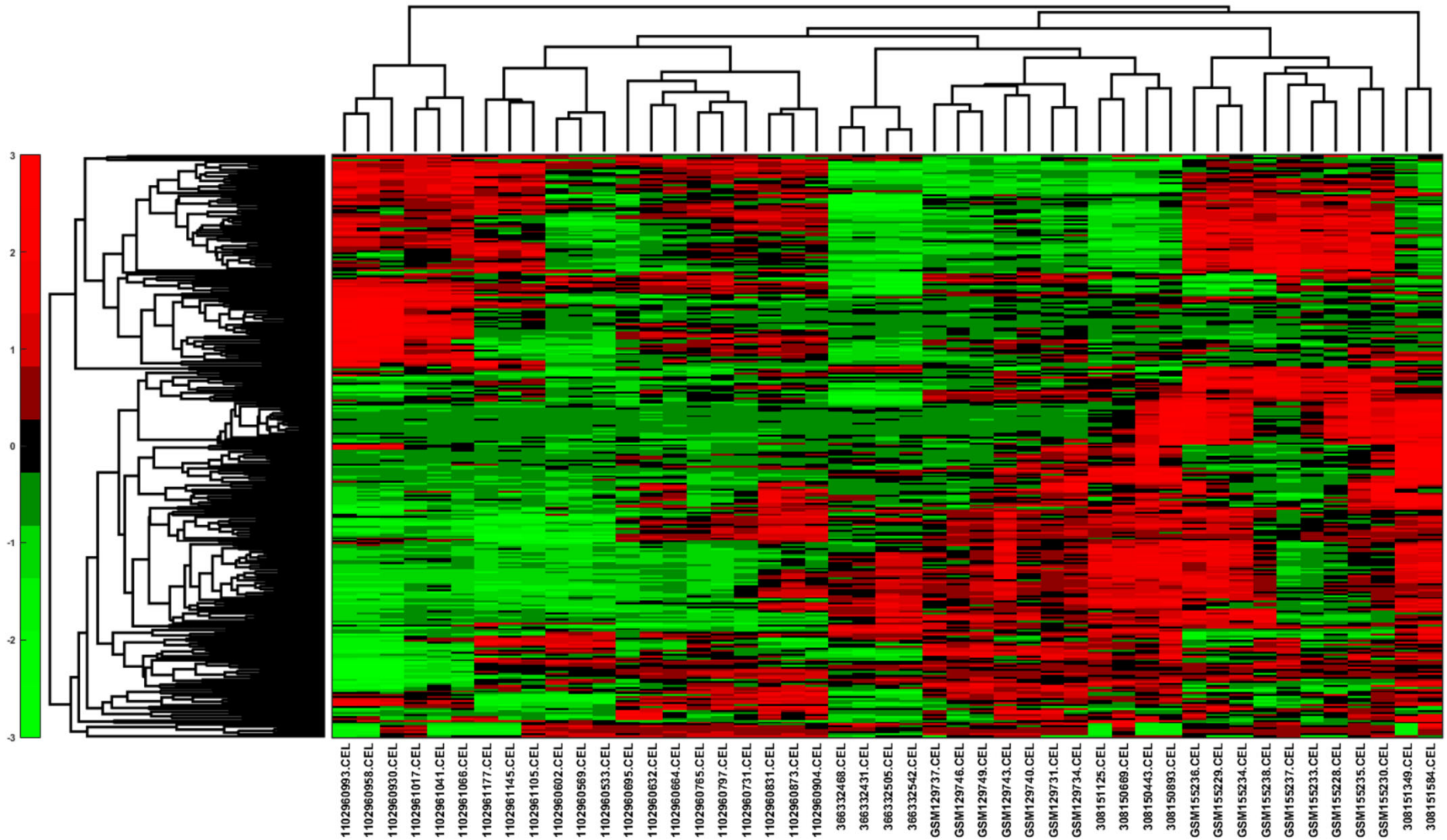
```
load expression_table.mat
gene_variation=std(exp_t)';
[a,b]=sort(gene_variation,'descend');
ngenest=100;
exp_t1=exp_t(b(1:ngenest),:);
gene_names1=gene_names(b(1:ngenest));
%%% for group 1
CGobj1 = clustergram(exp_t1,
'Standardize','Row',...
'RowLabels',
gene_names1,'ColumnLabels',array_names)
set(CGobj1,'RowLabels',gene_names1,'ColumnLabels',array_names,'linkage',
'average','RowPDist','euclidean');
set(CGobj1,'RowLabels',gene_names1,'ColumnLabels',array_names,'linkage',
'average','RowPDist','correlation');
```

Before clustering



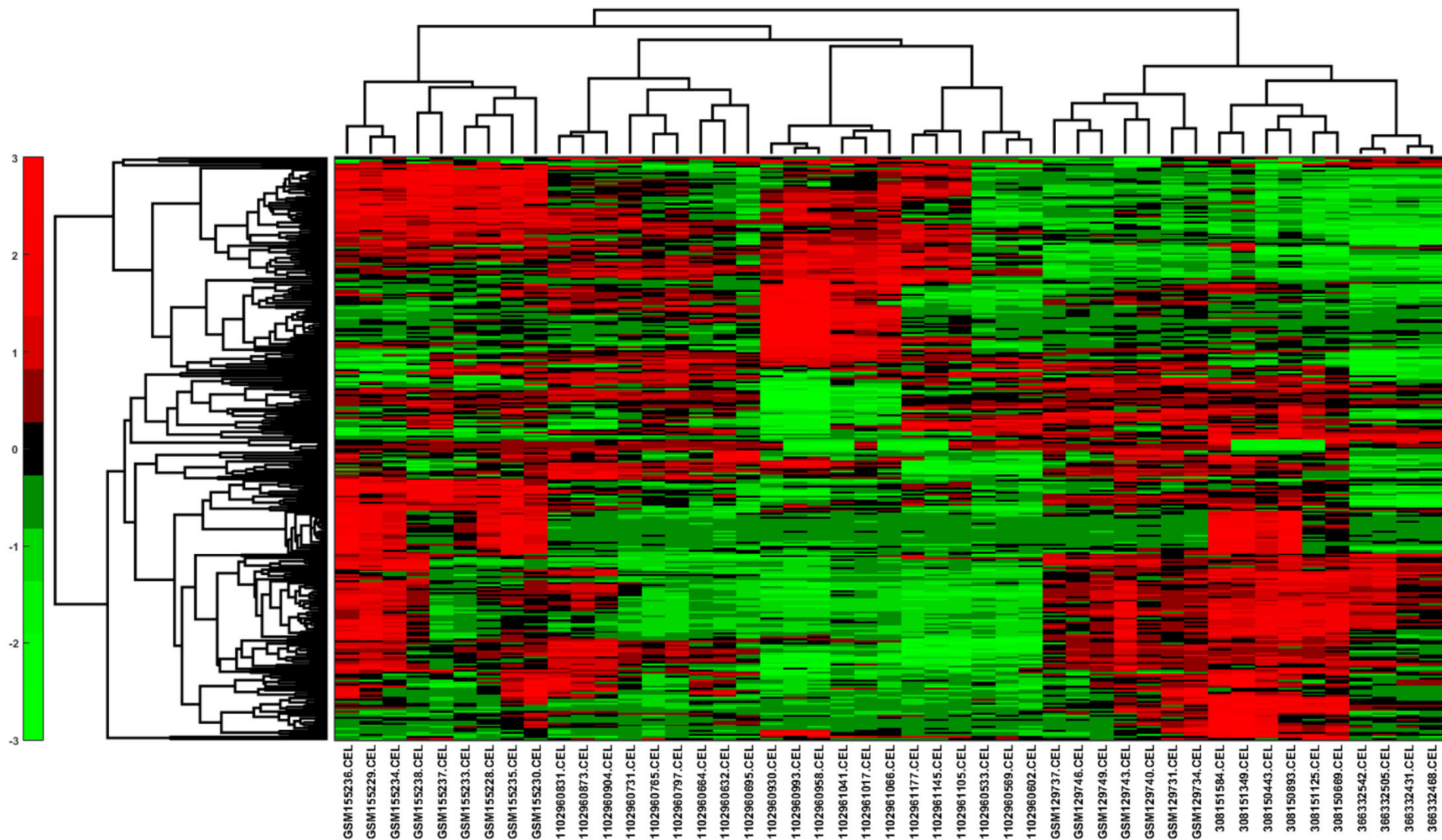


# UPGMA hierarchical clustering, Euclidian distance





# UPGMA hierarchical clustering, correlation distance



# Search for shared biological functions

- copy the list of displayed genes
- go to "Start Analysis" on <https://david.ncifcrf.gov/tools.jsp>
- Paste genes from gene list displayed by Matlab into the box in the left panel of the website
- select ENSEMBL\_GENE\_ID and "gene list" radio button
- Click "Functional Annotation Clustering"
- Select groups in "Annotation Summary Results" which have many genes from your list. Definitely select "PUBMED\_ID" and interaction databases like "Biogrid"
- First look at "Functional Annotation Chart" rectangular button below to display all overrepresented terms. Sort by "Benjamini" correction for multiple hypotheses testing
- Select "Functional Annotation Clustering" rectangular button below to display annotation results for gene list broken into multiple groups (clusters) each with related biological functions
- Write down the # of genes in the cluster and the top functions in two most interesting clusters

**%%%**

**%Which biological functions are overrepresented in different clusters?**

**%1) Pick a cluster:**

**%2) Select a node on the tree of rows,**

**%3) Right click**

**%4) Choose “export group info” into the workspace**

**%5) Name it gene\_list**

**%Run the following two Matlab commands to display genes**

**g1=gene\_list.RowNodeNames;**

**for m=1:length(g1);**

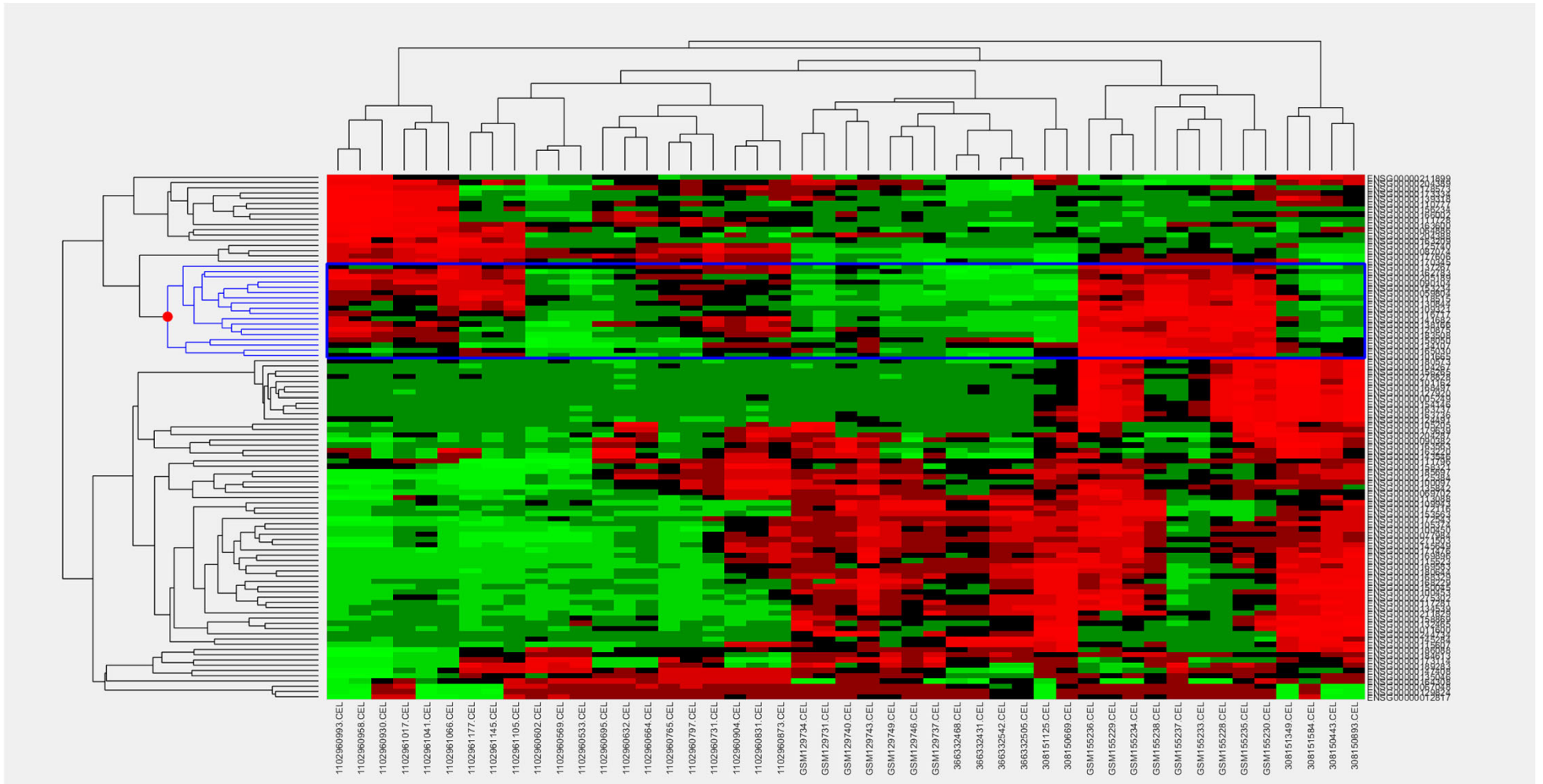
**disp(g1{m});**

**end;**

**% select ENSEMBL\_GENE\_ID and “gene list” radio button**  
**% Click "Functional Annotation Clustering"**  
**% Select groups in “Annotation Summary Results”**  
**% which have many genes from your list.**  
**% Definitely select “PUBMED\_ID” and**  
**% interaction databases like “Biogrid”**  
**% First look at "Functional Annotation Chart" rectangular button below**  
**% to display all overrepresented terms.**  
**% Sort by “Benjamini” correction for multiple hypotheses testing**  
**% Select "Functional Annotation Clustering" rectangular button below**  
**% to display annotation results for gene list broken into multiple groups**  
**% (clusters) each with related biological functions**  
**% Write down the # of genes in the cluster and the top functions**  
**% in two most interesting clusters**

# Using options:

'linkage', 'average', 'RowPDistValue', 'euclidean',



54 chart records

[Download File](#)

Sublist	Category	Term	RT	Genes	Count	%	P-Value	Benjamini
<input type="checkbox"/>	GOTERM_CC_DIRECT	<a href="#">nucleus</a>	RT		16	88.9	8.1E-7	3.7E-5
<input type="checkbox"/>	PIR_SUPERFAMILY	<a href="#">dual specificity protein phosphatase (MAP kinase phosphatase)</a>	RT		3	16.7	4.0E-5	8.0E-5
<input type="checkbox"/>	GOTERM_MF_DIRECT	<a href="#">protein tyrosine/threonine phosphatase activity</a>	RT		3	16.7	3.4E-5	1.3E-3
<input type="checkbox"/>	GOTERM_MF_DIRECT	<a href="#">MAP kinase tyrosine phosphatase activity</a>	RT		3	16.7	3.4E-5	1.3E-3
<input type="checkbox"/>	GOTERM_MF_DIRECT	<a href="#">MAP kinase tyrosine/serine/threonine phosphatase activity</a>	RT		3	16.7	5.9E-5	1.5E-3
<input type="checkbox"/>	INTERPRO	<a href="#">Mitogen-activated protein (MAP) kinase phosphatase</a>	RT		3	16.7	3.3E-5	1.9E-3
<input type="checkbox"/>	SMART	<a href="#">RHOD</a>	RT		3	16.7	2.5E-4	4.8E-3
<input type="checkbox"/>	INTERPRO	<a href="#">Rhodanese-like domain</a>	RT		3	16.7	2.2E-4	6.2E-3
<input type="checkbox"/>	SMART	<a href="#">DSPc</a>	RT		3	16.7	8.4E-4	8.0E-3
<input type="checkbox"/>	INTERPRO	<a href="#">Dual specificity phosphatase, catalytic domain</a>	RT		3	16.7	6.0E-4	9.2E-3
<input type="checkbox"/>	INTERPRO	<a href="#">Dual specificity phosphatase, subgroup, catalytic domain</a>	RT		3	16.7	6.6E-4	9.2E-3
<input type="checkbox"/>	GOTERM_BP_DIRECT	<a href="#">endoderm formation</a>	RT		3	16.7	5.6E-5	1.1E-2
<input type="checkbox"/>	UP_KW_CELLULAR_COMPONENT	<a href="#">Nucleus</a>	RT		13	72.2	1.5E-3	1.3E-2
<input type="checkbox"/>	SMART	<a href="#">PTPc motif</a>	RT		3	16.7	2.3E-3	1.5E-2
<input type="checkbox"/>	GOTERM_MF_DIRECT	<a href="#">phosphoprotein phosphatase activity</a>	RT		3	16.7	8.0E-4	1.5E-2
<input type="checkbox"/>	INTERPRO	<a href="#">Protein-tyrosine phosphatase, catalytic</a>	RT		3	16.7	1.4E-3	1.6E-2
<input type="checkbox"/>	UP_KW_PTM	<a href="#">Ubl conjugation</a>	RT		7	38.9	4.5E-3	1.9E-2
<input type="checkbox"/>	UP_KW_PTM	<a href="#">Isopeptide bond</a>	RT		6	33.3	5.4E-3	1.9E-2
<input type="checkbox"/>	INTERPRO	<a href="#">Protein-tyrosine phosphatase, active site</a>	RT		3	16.7	2.1E-3	2.0E-2
<input type="checkbox"/>	INTERPRO	<a href="#">Protein-tyrosine/Dual specificity phosphatase</a>	RT		3	16.7	2.8E-3	2.3E-2
<input type="checkbox"/>	UP_SEQ_FEATURE	DOMAIN:Rhodanese	RT		3	16.7	1.9E-4	2.4E-2
<input type="checkbox"/>	KEGG_PATHWAY	<a href="#">MAPK signaling pathway</a>	RT		5	27.8	5.9E-4	2.8E-2
<input type="checkbox"/>	GOTERM_MF_DIRECT	<a href="#">myosin phosphatase activity</a>	RT		3	16.7	2.4E-3	3.6E-2
<input type="checkbox"/>	GOTERM_MF_DIRECT	<a href="#">protein tyrosine phosphatase activity</a>	RT		3	16.7	4.2E-3	5.3E-2
<input type="checkbox"/>	GOTERM_CC_DIRECT	<a href="#">nucleoplasm</a>	RT		10	55.6	2.3E-3	5.4E-2
<input type="checkbox"/>	GOTERM_BP_DIRECT	<a href="#">negative regulation of MAPK cascade</a>	RT		3	16.7	7.0E-4	6.8E-2



Gene list being analyzed

Clustering options and stringency

score for the group based on the EASE scores of each term members. The higher, the more enriched.

ALL genes involved in this annotation cluster

Every term in the annotation cluster

Genes involved in individual term

Related Term Search

Options Classification Stringency High

Rerun using options Create Sublist Download File

A group of terms having similar biological meaning due to sharing similar gene members

Annotation Cluster 1		Enrichment Score: 3.69			
<input type="checkbox"/>	SP_PIR_KEYWORDS	<a href="#">chromoprotein</a>	RT	7	1.1E-5
<input type="checkbox"/>	SP_PIR_KEYWORDS	<a href="#">metalloprotein</a>	RT	8	4.7E-5
<input type="checkbox"/>	SP_PIR_KEYWORDS	<a href="#">iron</a>	RT	9	2.1E-4
<input type="checkbox"/>	GOTERM_MF_ALL	<a href="#">iron ion binding</a>	RT	10	2.5E-4
<input type="checkbox"/>	SP_PIR_KEYWORDS	<a href="#">heme</a>	RT	7	3.5E-4
<input type="checkbox"/>	GOTERM_MF_ALL	<a href="#">tetrapyrrole binding</a>	RT	6	1.3E-3
<input type="checkbox"/>	GOTERM_MF_ALL	<a href="#">heme binding</a>	RT	6	1.3E-3
Annotation Cluster 2		Enrichment Score: 3.52			
<input type="checkbox"/>	SP_PIR_KEYWORDS	<a href="#">antibiotic</a>	RT	5	2.2E-4
<input type="checkbox"/>	SP_PIR_KEYWORDS	<a href="#">antimicrobial</a>	RT	5	2.4E-4
<input type="checkbox"/>	GOTERM_BP_ALL	<a href="#">defense response to bacteria</a>	RT	6	5.4E-4
Annotation Cluster 3		Enrichment Score: 2.66			
<input type="checkbox"/>	UP_SEQ_FEATURE	domain:Ig-like C2-type 1	RT	8	5.4E-4
<input type="checkbox"/>	UP_SEQ_FEATURE	domain:Ig-like C2-type 2	RT	8	5.4E-4
<input type="checkbox"/>	INTERPRO_NAME	<a href="#">Immunoglobulin</a>	RT	6	3.6E-2
Annotation Cluster 4		Enrichment Score: 2.63			

EASE Score, the modified Fisher Exact P-Value. They are identical to that in the Chart Report. The smaller, the more enriched.

# Functional Annotation Clustering

[Help and Manual](#)

Current Gene List: List\_3






















Current Background: Homo sapiens

18 DAVID IDs






























Options Classification Stringency Medium






























## 25 Cluster(s)

[Download File](#)

Annotation Cluster 1	Enrichment Score: 5.2	<span style="color: red;">G</span>		Count	P_Value	Benjamini
<input type="checkbox"/> DISGENET	<a href="#">Juvenile arthritis</a>	<a href="#">RT</a>		7	1.5E-8	4.7E-7
<input type="checkbox"/> DISGENET	<a href="#">Juvenile psoriatic arthritis</a>	<a href="#">RT</a>		7	1.5E-8	4.7E-7
<input type="checkbox"/> DISGENET	<a href="#">Polyarthritis, Juvenile, Rheumatoid Factor Negative</a>	<a href="#">RT</a>		7	1.5E-8	4.7E-7
<input type="checkbox"/> DISGENET	<a href="#">Polyarthritis, Juvenile, Rheumatoid Factor Positive</a>	<a href="#">RT</a>		7	1.5E-8	4.7E-7
<input type="checkbox"/> DISGENET	<a href="#">Juvenile-Onset Still Disease</a>	<a href="#">RT</a>		7	1.8E-8	4.7E-7
<input type="checkbox"/> KEGG_PATHWAY	<a href="#">MAPK signaling pathway</a>	<a href="#">RT</a>		5	5.9E-4	2.8E-2
<input type="checkbox"/> BIOGRID_INTERACTION	<a href="#">mitogen-activated protein kinase 1(MAPK1)</a>	<a href="#">RT</a>		4	3.8E-3	1.0E0
<input type="checkbox"/> WIKIPATHWAYS	<a href="#">MAPK signaling pathway</a>	<a href="#">RT</a>		3	5.8E-2	6.9E-1
<input type="checkbox"/> GAD_DISEASE_CLASS	UNKNOWN	<a href="#">RT</a>		5	1.5E-1	9.9E-1
Annotation Cluster 2	Enrichment Score: 2.83	<span style="color: red;">G</span>		Count	P_Value	Benjamini
<input type="checkbox"/> INTERPRO	<a href="#">Mitogen-activated protein (MAP) kinase phosphatase</a>	<a href="#">RT</a>		3	3.3E-5	1.9E-3
<input type="checkbox"/> GOTERM_MF_DIRECT	<a href="#">protein tyrosine/threonine phosphatase activity</a>	<a href="#">RT</a>		3	3.4E-5	1.3E-3
<input type="checkbox"/> GOTERM_MF_DIRECT	<a href="#">MAP kinase tyrosine phosphatase activity</a>	<a href="#">RT</a>		3	3.4E-5	1.3E-3
<input type="checkbox"/> PIR_SUPERFAMILY	<a href="#">dual specificity protein phosphatase (MAP kinase phosphatase)</a>	<a href="#">RT</a>		3	4.0E-5	8.0E-5
<input type="checkbox"/> GOTERM_BP_DIRECT	<a href="#">endoderm formation</a>	<a href="#">RT</a>		3	5.6E-5	1.1E-2
<input type="checkbox"/> GOTERM_MF_DIRECT	<a href="#">MAP kinase tyrosine/serine/threonine phosphatase activity</a>	<a href="#">RT</a>		3	5.9E-5	1.5E-3
<input type="checkbox"/> PUBMED_ID	<a href="#">27880917</a>	<a href="#">RT</a>		4	1.7E-4	2.5E-2
<input type="checkbox"/> UP_SEQ_FEATURE	DOMAIN:Rhodanese	<a href="#">RT</a>		3	1.9E-4	2.4E-2
<input type="checkbox"/> INTERPRO	<a href="#">Rhodanese-like domain</a>	<a href="#">RT</a>		3	2.2E-4	6.2E-3
<input type="checkbox"/> SMART	RHOD	<a href="#">RT</a>		3	2.5E-4	4.8E-3



Annotation Cluster 3		Enrichment Score: 2.43	G		Count	P_Value	Benjamini
<input type="checkbox"/>	DISGENET	<a href="#">Arsenic Poisoning, Inorganic</a>	RT		3	3.5E-3	4.6E-2
<input type="checkbox"/>	DISGENET	<a href="#">Nervous System, Organic Arsenic Poisoning</a>	RT		3	3.5E-3	4.6E-2
<input type="checkbox"/>	DISGENET	<a href="#">Arsenic Poisoning</a>	RT		3	3.5E-3	4.6E-2
<input type="checkbox"/>	DISGENET	<a href="#">Arsenic Encephalopathy</a>	RT		3	3.5E-3	4.6E-2
<input type="checkbox"/>	DISGENET	<a href="#">Arsenic Induced Polyneuropathy</a>	RT		3	3.5E-3	4.6E-2
<input type="checkbox"/>	DISGENET	<a href="#">Dermatologic disorders</a>	RT		3	5.1E-3	5.6E-2
Annotation Cluster 4		Enrichment Score: 2.26	G		Count	P_Value	Benjamini
<input type="checkbox"/>	PUBMED_ID	<a href="#">19322201</a>	RT		7	1.3E-8	5.9E-6
<input type="checkbox"/>	BIOGRID_INTERACTION	<a href="#">ELAV like RNA binding protein 1(ELAVL1)</a>	RT		7	4.4E-3	1.0E0
<input type="checkbox"/>	UCSC_TFBS	CEBPA	RT		7	1.8E-1	1.0E0
<input type="checkbox"/>	UCSC_TFBS	CDPCR3HD	RT		7	6.5E-1	1.0E0
<input type="checkbox"/>	UCSC_TFBS	FOXD3	RT		5	7.4E-1	1.0E0
Annotation Cluster 5		Enrichment Score: 2.14	G		Count	P_Value	Benjamini
<input type="checkbox"/>	GOTERM_BP_DIRECT	<a href="#">negative regulation of transcription from RNA polymerase II promoter</a>	RT		6	1.4E-3	9.1E-2
<input type="checkbox"/>	BIOGRID_INTERACTION	<a href="#">retinoid X receptor alpha(RXRA)</a>	RT		3	6.1E-3	1.0E0
<input type="checkbox"/>	GOTERM_MF_DIRECT	<a href="#">protein heterodimerization activity</a>	RT		3	4.5E-2	3.7E-1
Annotation Cluster 6		Enrichment Score: 1.95	G		Count	P_Value	Benjamini
<input type="checkbox"/>	REACTOME_PATHWAY	<a href="#">Generic Transcription Pathway</a>	RT		7	2.8E-3	1.7E-1
<input type="checkbox"/>	REACTOME_PATHWAY	<a href="#">RNA Polymerase II Transcription</a>	RT		7	4.6E-3	1.7E-1
<input type="checkbox"/>	REACTOME_PATHWAY	<a href="#">Gene expression (Transcription)</a>	RT		7	8.2E-3	2.0E-1
<input type="checkbox"/>	GAD_DISEASE_CLASS	UNKNOWN	RT		5	1.5E-1	9.9E-1
Annotation Cluster 7		Enrichment Score: 1.76	G		Count	P_Value	Benjamini
<input type="checkbox"/>	PUBMED_ID	<a href="#">18029348</a>	RT		6	1.8E-5	3.4E-3
<input type="checkbox"/>	UP_KW_PTM	<a href="#">Isopeptide bond</a>	RT		6	5.4E-3	1.9E-2
<input type="checkbox"/>	PUBMED_ID	<a href="#">15342556</a>	RT		3	7.9E-3	4.8E-1
<input type="checkbox"/>	PUBMED_ID	<a href="#">26496610</a>	RT		3	1.0E-1	1.0E0
<input type="checkbox"/>	GOTERM_MF_DIRECT	<a href="#">metal ion binding</a>	RT		4	4.5E-1	1.0E0
<input type="checkbox"/>	UCSC_TFBS	TAL1ALPHAE47	RT		3	7.9E-1	1.0E0

Annotation Cluster 3		Enrichment Score: 2.43	G		Count	P_Value	Benjamini
<input type="checkbox"/>	DISGENET	<a href="#">Arsenic Poisoning, Inorganic</a>	RT		3	3.5E-3	4.6E-2
<input type="checkbox"/>	DISGENET	<a href="#">Nervous System, Organic Arsenic Poisoning</a>	RT		3	3.5E-3	4.6E-2
<input type="checkbox"/>	DISGENET	<a href="#">Arsenic Poisoning</a>	RT		3	3.5E-3	4.6E-2
<input type="checkbox"/>	DISGENET	<a href="#">Arsenic Encephalopathy</a>	RT		3	3.5E-3	4.6E-2
<input type="checkbox"/>	DISGENET	<a href="#">Arsenic Induced Polyneuropathy</a>	RT		3	3.5E-3	4.6E-2
<input type="checkbox"/>	DISGENET	<a href="#">Dermatologic disorders</a>	RT		3	5.1E-3	5.6E-2
Annotation Cluster 4		Enrichment Score: 2.26	G		Count	P_Value	Benjamini
<input type="checkbox"/>	PUBMED_ID	<a href="#">19322201</a>	RT		7	1.3E-8	5.9E-6
<input type="checkbox"/>	BIOGRID_INTERACTION	<a href="#">ELAV like RNA binding protein 1(ELAVL1)</a>	RT		7	4.4E-3	1.0E0
<input type="checkbox"/>	UCSC_TFBS	CEBPA	RT		7	1.8E-1	1.0E0
<input type="checkbox"/>	UCSC_TFBS	CDPCR3HD	RT		7	6.5E-1	1.0E0
<input type="checkbox"/>	UCSC_TFBS	FOXO3	RT		5	7.4E-1	1.0E0
Annotation Cluster 5		Enrichment Score: 2.14	G		Count	P_Value	Benjamini
<input type="checkbox"/>	GOTERM_BP_DIRECT	<a href="#">negative regulation of transcription from RNA polymerase II promoter</a>	RT		6	1.4E-3	9.1E-2
<input type="checkbox"/>	BIOGRID_INTERACTION	<a href="#">retinoid X receptor alpha(RXRA)</a>	RT		3	6.1E-3	1.0E0
<input type="checkbox"/>	GOTERM_MF_DIRECT	<a href="#">protein heterodimerization activity</a>	RT		3	4.5E-2	3.7E-1
Annotation Cluster 6		Enrichment Score: 1.95	G		Count	P_Value	Benjamini
<input type="checkbox"/>	REACTOME_PATHWAY	<a href="#">Generic Transcription Pathway</a>	RT		7	2.8E-3	1.7E-1
<input type="checkbox"/>	REACTOME_PATHWAY	<a href="#">RNA Polymerase II Transcription</a>	RT		7	4.6E-3	1.7E-1
<input type="checkbox"/>	REACTOME_PATHWAY	<a href="#">Gene expression (Transcription)</a>	RT		7	8.2E-3	2.0E-1
<input type="checkbox"/>	GAD_DISEASE_CLASS	UNKNOWN	RT		5	1.5E-1	9.9E-1
Annotation Cluster 7		Enrichment Score: 1.76	G		Count	P_Value	Benjamini
<input type="checkbox"/>	PUBMED_ID	<a href="#">18029348</a>	RT		6	1.8E-5	3.4E-3
<input type="checkbox"/>	UP_KW_PTM	<a href="#">Isopeptide bond</a>	RT		6	5.4E-3	1.9E-2
<input type="checkbox"/>	PUBMED_ID	<a href="#">15342556</a>	RT		3	7.9E-3	4.8E-1
<input type="checkbox"/>	PUBMED_ID	<a href="#">26496610</a>	RT		3	1.0E-1	1.0E0
<input type="checkbox"/>	GOTERM_MF_DIRECT	<a href="#">metal ion binding</a>	RT		4	4.5E-1	1.0E0
<input type="checkbox"/>	UCSC_TFBS	TAL1ALPHA47	RT		3	7.9E-1	1.0E0

Credit: XKCD  
comics

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WHY ARE THERE GHOSTS



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WHY DO SPIDERS COME INSIDE

WHY ARE THERE HUGE SPIDERS IN MY HOUSE

WHY ARE THERE LOTS OF SPIDERS IN MY HOUSE

WHY ARE THERE SPIDERS IN MY ROOM

WHY ARE THERE SO MANY SPIDERS IN MY ROOM

WHY DO SPIDER BITES ITCH

WHY IS DYING SO SCARY

WHY IS THERE NO GPS IN LAPTOPS

WHY DO KNEES CLICK

WHY AREN'T THERE E GRADES

WHY IS SEX SO IMPORTANT



WHY IS MT VESUVIUS THERE

WHY DO THEY SAY T MINUS

WHY ARE THERE OBELISKS

WHY ARE WRESTLERS ALWAYS WET

WHY ARE OCEANS BECOMING MORE ACIDIC

WHY IS ARWEN DYING

WHY AREN'T MY QUAIL LAYING EGGS

WHY AREN'T MY QUAIL EGGS HATCHING

WHY ARE ULTRASOUNDS IMPORTANT

WHY ARE ULTRASOUND MACHINES EXPENSIVE

WHY IS STEALING WRONG

WHY AREN'T THERE GUNS IN HARRY POTTER

WHY AREN'T THERE ANY FOREIGN MILITARY BASES IN AMERICA

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WHY IS THERE A 0 OHM RESISTOR

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WHY DO RHYMES SOUND GOOD

WHY DO TREES DIE

WHY IS THERE HELL IF GOD FORGIVES

WHY DO IGUANAS DIE  
WHY AREN'T THERE DINOSAUR GHOSTS

WHY ARE THERE FEMALE MR NIMES

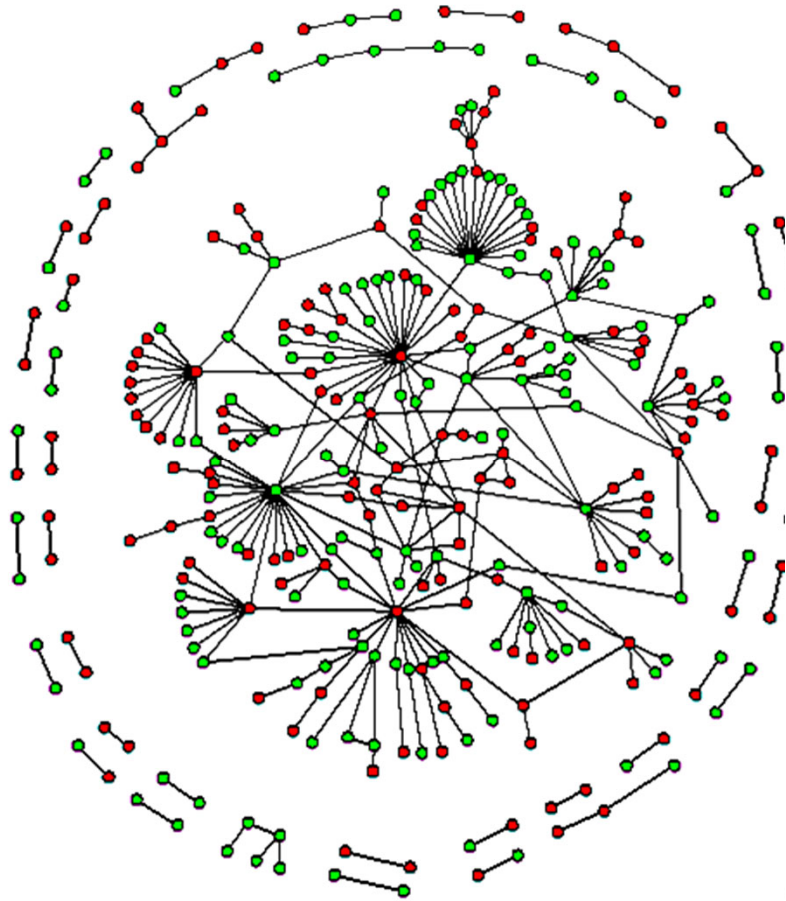
WHY IS GPS FREE

# Basic concepts of network analysis

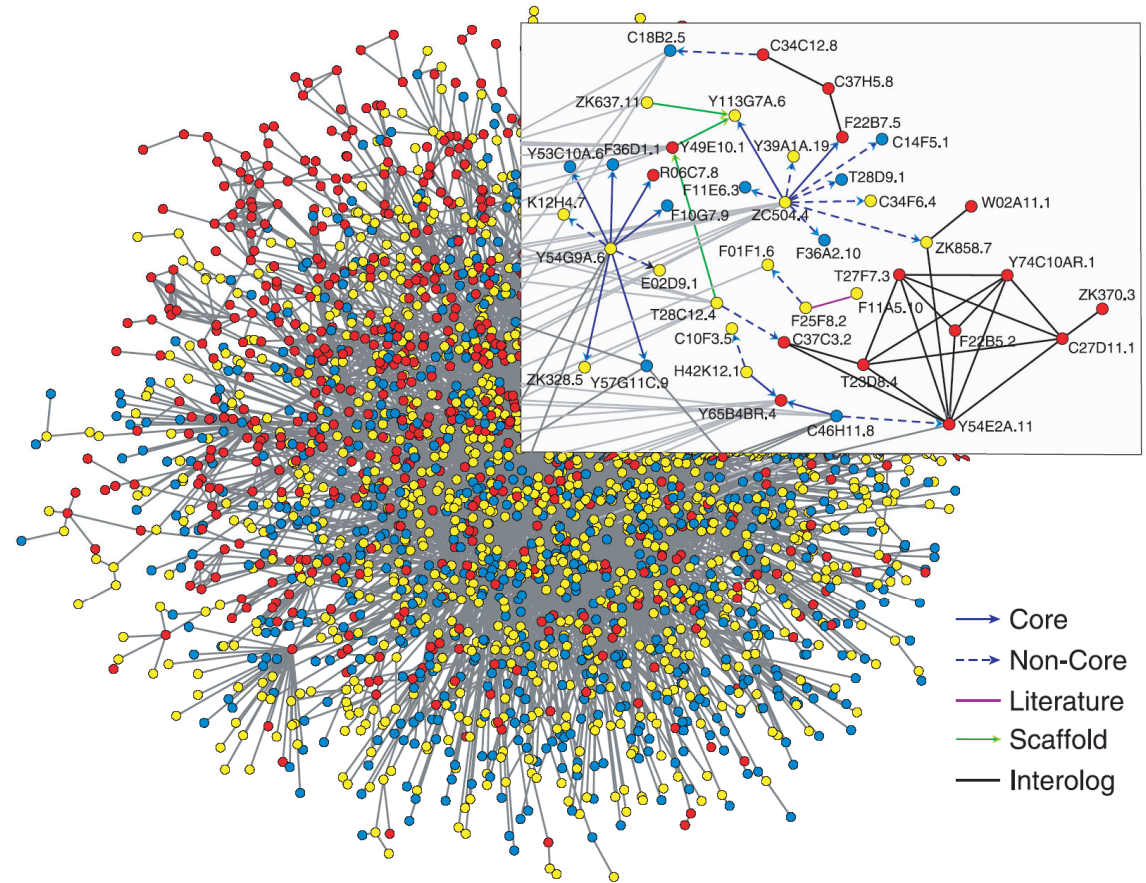
Reminder from the first lecture



# Protein-Protein binding IntAct Database (Dec 2015) Interactions: 577,297 Proteins: 89,716

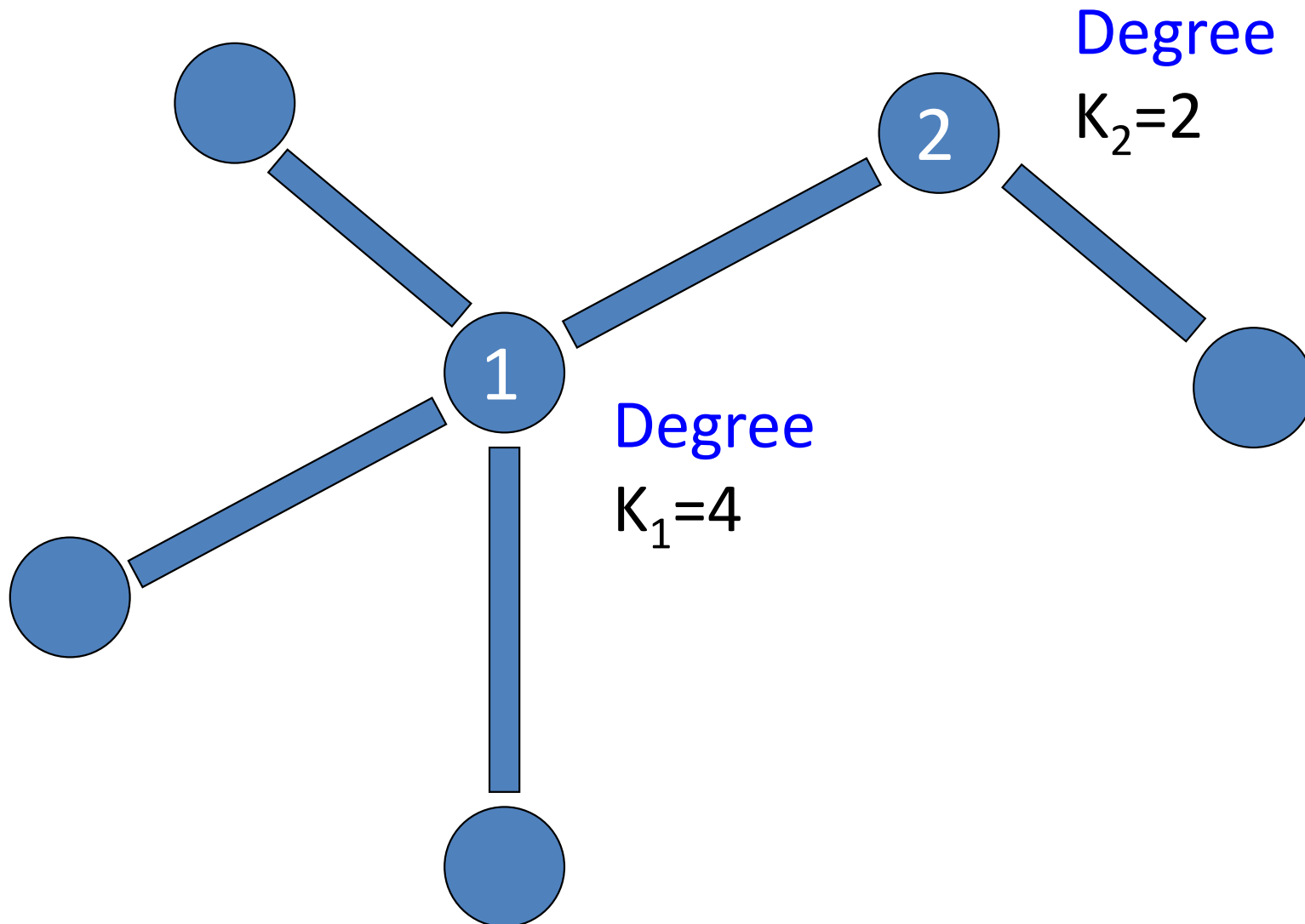


Baker's yeast *S. cerevisiae* (only nuclear proteins shown)  
From S. Maslov, K. Sneppen, Science 2002

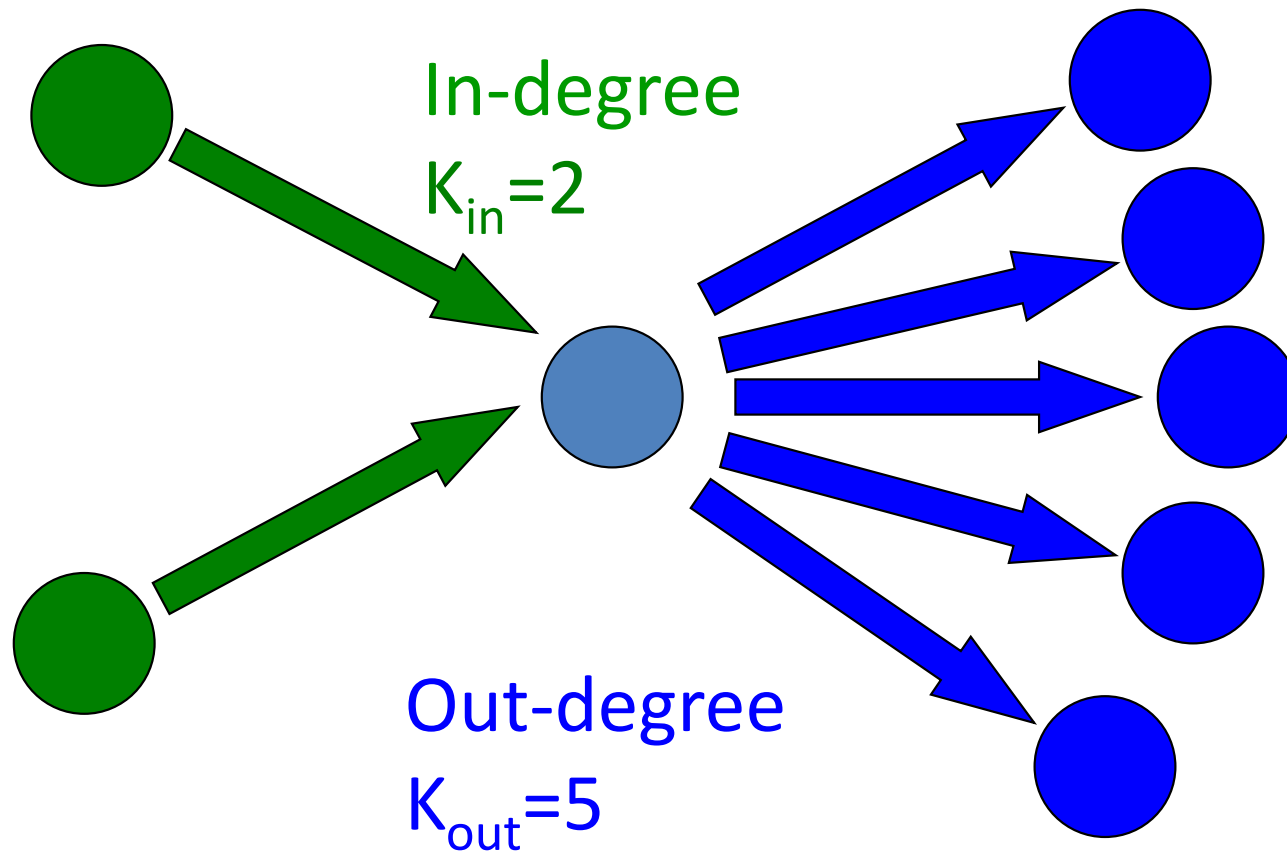


Worm *C. elegans*  
From S. Lee et al, Science 2004

# Degree of a node – its # of neighbors



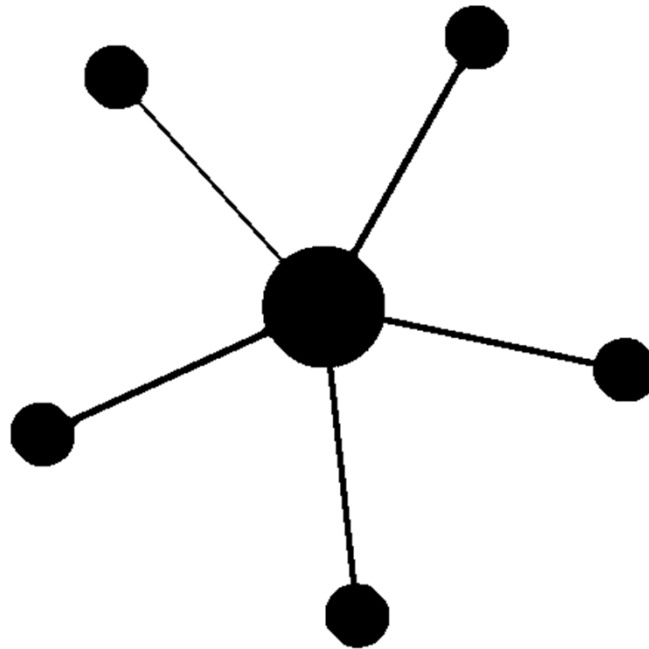
# Directed networks have in- and out- degrees





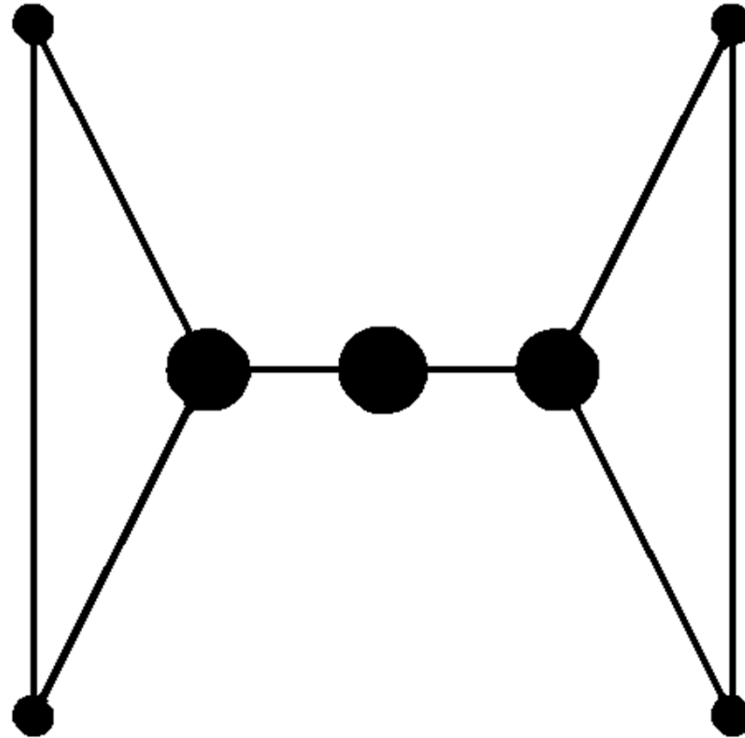
# How to find “important” nodes?

- By their degree
- Hubs = important
- Example: Google’s PageRank



# How to find “important” nodes?

- By their connectivity
- Connectors = important
- Betweenness-centrality

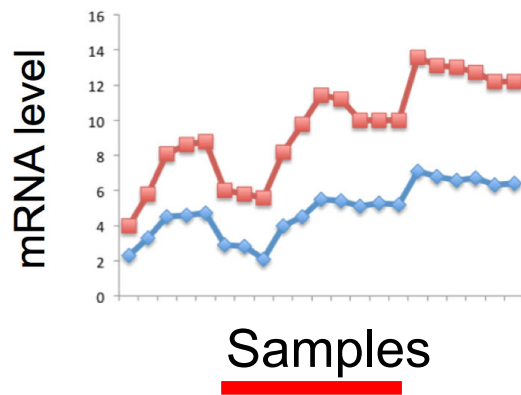


# Betweenness centrality: definition

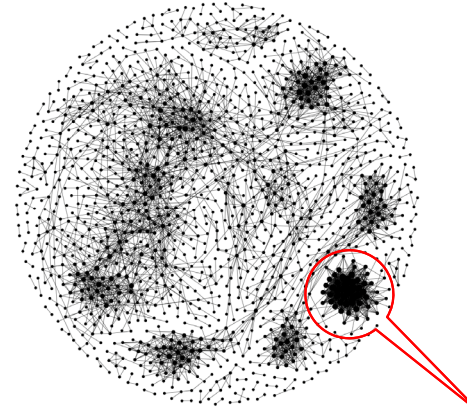
- Take a node  $i$
- There are  $(N-1)*(N-2)/2$  pairs of other nodes
- For each pair find the shortest path on the network
- If more than one shortest path, sample them equally
- Betweenness-centrality  $C(i) \sim$  the number of shortest paths going through node  $i$

To analyze  
correlations in expression  
for all pairs of genes:  
**Co-expression networks**

# How to construct a co-expression network?



A co-expression network



Functional modules

- Start with a matrix of log2 of expression levels of N genes in K samples (conditions): for our T-cell data N=3000, K=47
- For each of  $N(N-1)/2$  pairs of genes  $i$  and  $j$  calculate the correlation coefficient  $\rho_{ij} = \sigma_{ij} / \sigma_i \sigma_j$  of gene levels across K samples
- Put a threshold, e.g.  $\rho_{ij} > 0.85$ , or otherwise select the most correlated pairs of genes (~4500 in our case). Now you have a weighted network.
- Identify densely interconnected functional modules in this network.
- Modules can be used to infer unknown functions of genes via “Guilt by Association” principle.

# How to install Gephi software for network analysis?

- Install Gephi from: <https://gephi.org/users/download/>
- One of the common problems with installation is the version of Java on your computer. One possible solution is here: <https://github.com/gephi/gephi/issues/1787>.

Sometimes after installation Gephi may complain that it cannot find java version 1.8 or higher. In this case you need to go to C:\Program Files\Gephi-0.9.2\etc

Open file gephi.conf using notepad.exe (MS Word does not work!).

Add a line `jdkhome="C:\Program Files (x86)\Java\jre1.8.0_231"`

(the numbers in ...jre1.8.0\_231 may be changed to reflect the actual directory where Java is installed on your computer).

If JDK is not installed on your computer, you need to install it first from <https://www.java.com/en/download/win10.jsp>

# Co-expression network analysis exercise

- Start Gephi and open [coexpression\\_network\\_random\\_start.gexi](#)
- Run “Layout” → Fruchterman Reingold → Speed 10.0
- Run “Average degree”, “Network diameter”, “Modularity” in the Statistics tab in the right panel.
- Color nodes by “modularity class”:  
Appearance → Nodes → Partition → Palette Icon → Modularity class
- Size nodes first by “degree”.  
Appearance → Nodes → Ranking → Multiple Circles Icon → Degree
  - If the nodes are too small, select “Min size”: 10 and “Max size”:80
  - Nodes in large tightly connected clusters have large degree
- Then size nodes by “betweenness-centrality”  
Appearance → Nodes → Ranking → Multiple Circles Icon → Betweenness-centrality
  - Large circles are “coordinator” genes connecting different co-expressed clusters to each other. Potentially biologically interesting

# Disease-disease similarity network

- Based on the table summarizing all current medical knowledge of genes implicated in diseases:
  - Rows: 516 common human diseases
  - Columns: 25,000 human genes
  - Matrix element  $D_{i\alpha} = 1$  if the gene  $\alpha$  is known to be involved in the disease  $i$ . 0 – otherwise
- Constructed disease-disease similarity network:
  - Weight of the edge - # of shared genes between two diseases
  - Easy to construct: the adjacency matrix  $A$  of the network is simply  $A = D \cdot D^+$



# Disease network analysis exercise

- Start Gephi and open `disease_disease_random_start.gexi`
- Run “Layout” → Fruchterman Reingold → Speed 10.0  
Observe how clusters emerge.
- Run “Average degree”, “Network diameter”, “Modularity” analysis tools in the right panel.
- Color nodes with **medical term: “disorder class”**  
Appearance → Nodes → Partition → Palette Icon → Disorder class
- Then color nodes by “modularity class”. See how well it agrees with the previous color.  
Appearance → Nodes → Partition → Palette Icon → Modularity class
- Size nodes first by “**degree**”.  
Appearance → Nodes → Ranking → Multiple Circles Icon → Degree
  - Which disease has the largest degree?
- Size nodes by “**betweenness centrality**”  
Appearance → Nodes → Ranking → Multiple Circles Icon → Degree
  - Which diseases have the largest betweenness-centrality?  
These “connector” diseases linking different diseases clusters to each other. They highlight potentially interesting connections between diseases

Credit: XKCD  
comics

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WHY ARE THERE BRIDESMAIDS  
WHY DO DYING PEOPLE REACH UP  
WHY AREN'T THERE VARICOSE ARTERIES  
WHY ARE OLD KUNGONS DIFFERENT



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WHY DO SPIDERS COME INSIDE  
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WHY DO DREAMS SEEM SO REAL

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WHY AREN'T THERE E GRADES  
WHY IS ISOLATION BAD  
WHY DO BOYS LIKE ME  
WHY DON'T BOYS LIKE ME  
WHY IS THERE ALWAYS A JAVA UPDATE  
WHY ARE THERE RED DOTS ON MY THIGHS  
WHY IS LYING GOOD



WHY IS GPS FREE