

Review for the Final Exam

Ask me questions about HW1-4
you can ask me directly in chat

Final exam

- The final exam for BIOE 310 will be held in **our usual room:** 4025 Campus Instructional Facility
- It will be a **2 hours exam:**
5/07/2024, Tuesday, 7:00 PM-9:00 PM

Rules

- **Closed book exam**; no books, notes, laptops, smartphones, etc.
- However, **calculators** (not on a smartphone) **can be used**.
- You can prepare **one cheat sheet** (letter size, two-sided if needed)
- Printouts provided:
 - Distributions means/variances/pdfs
 - Standard normal distribution CDF table

Name	Probability Distribution	Mean	Variance	Section in Book
Discrete				
Uniform	$\frac{1}{n}, a \leq b$	$\frac{(b+a)}{2}$	$\frac{(b-a+1)^2-1}{12}$	3-5
Binomial	$\binom{n}{x} p^x (1-p)^{n-x}$ $x = 0, 1, \dots, n, 0 \leq p \leq 1$	np	$np(1-p)$	3-6
Geometric	$(1-p)^{x-1} p$ $x = 1, 2, \dots, 0 \leq p \leq 1$	$1/p$	$(1-p)/p^2$	3-7.1
Negative binomial	$\binom{x-1}{r-1} (1-p)^{x-r} p^r$ $x = r, r+1, r+2, \dots, 0 \leq p \leq 1$	r/p	$r(1-p)/p^2$	3-7.2

This will be provided

Poisson	$\frac{e^{-\lambda} \lambda^x}{x!}, x = 0, 1, 2, \dots, 0 < \lambda$	λ	λ	3-9
Continuous				
Uniform	$\frac{1}{b-a}, a \leq x \leq b$	$\frac{(b+a)}{2}$	$\frac{(b-a)^2}{12}$	4-5
Normal	$\frac{1}{\sigma\sqrt{2\pi}} e^{-1/2(\frac{x-\mu}{\sigma})^2}$ $-\infty < x < \infty, -\infty < \mu < \infty, 0 < \sigma$	μ	σ^2	4-6
Exponential	$\lambda e^{-\lambda x}, 0 \leq x, 0 < \lambda$	$1/\lambda$	$1/\lambda^2$	4-8
Erlang	$\frac{\lambda^r x^{r-1} e^{-\lambda x}}{(r-1)!}, 0 < x, r = 1, 2, \dots$	r/λ	r/λ^2	4-9.1
Gamma	$\frac{\lambda^r x^{r-1} e^{-\lambda x}}{\Gamma(r)}, 0 < x, 0 < r, 0 < \lambda$	r/λ	r/λ^2	4-9.2

z	0.00	0.01	0.02	0.03	0.04	0.05	0.06	0.07	0.08	0.09
0.0	0.500000	0.503989	0.507978	0.511967	0.515953	0.519939	0.523922	0.527903	0.531881	0.535856
0.1	0.539828	0.543795	0.547758	0.551717	0.555670	0.559618	0.563559	0.567495	0.571424	0.575345
0.2	0.579260	0.583166	0.587064	0.590954	0.594835	0.598706	0.602568	0.606420	0.610261	0.614092
0.3	0.617911	0.621719	0.625516	0.629300	0.633072	0.636831	0.640576	0.644309	0.648027	0.651732
0.4	0.655422	0.659097	0.662757	0.666402	0.670031	0.673645	0.677242	0.680822	0.684386	0.687933
0.5	0.691462	0.694974	0.698468	0.701944	0.705401	0.708840	0.712260	0.715661	0.719043	0.722405
0.6	0.725747	0.729069	0.732371	0.735653	0.738914	0.742154	0.745373	0.748571	0.751748	0.754903
0.7	0.758036	0.761148	0.764238	0.767305	0.770350	0.773373	0.776373	0.779350	0.782305	0.785236
0.8	0.788145	0.791030	0.793892	0.796731	0.799546	0.802338	0.805106	0.807850	0.810570	0.813267
0.9	0.815940	0.818589	0.821214	0.823815	0.826391	0.828944	0.831472	0.833977	0.836457	0.838913
1.0	0.841345	0.843752	0.846136	0.848495	0.850830	0.853141	0.855428	0.857690	0.859929	0.862143
1.1	0.864334	0.866500	0.868643	0.870762	0.872857	0.874928	0.876976	0.878999	0.881000	0.882977
1.2	0.884930	0.886860	0.888767	0.890651	0.892512	0.894350	0.896165	0.897958	0.899727	0.901475
1.3	0.903199	0.904902	0.906582	0.908241	0.909877	0.911492	0.913085	0.914657	0.916207	0.917736
1.4	0.919243	0.920730	0.922196	0.923641	0.925066	0.926471	0.927855	0.929219	0.930563	0.931888
1.5	0.933193	0.934478	0.935744	0.936992	0.938220	0.939429	0.940620	0.941792	0.942947	0.944083
1.6	0.945201	0.946301	0.947384	0.948449	0.949497	0.950529	0.951543	0.952540	0.953521	0.954486
1.7	0.955435	0.956367	0.957284	0.958185	0.959071	0.959941	0.960796	0.961636	0.962462	0.963273
1.8	0.964070	0.964852	0.965621	0.966375	0.967116	0.967843	0.968557	0.969258	0.969946	0.970621
1.9	0.971283	0.971933	0.972571	0.973197	0.973810	0.974412	0.975002	0.975581	0.976148	0.976705
2.0	0.977250	0.977784	0.978308	0.978822	0.979325	0.979818	0.980301	0.980774	0.981237	0.981691
2.1	0.982136	0.982571	0.982997	0.983414	0.983823	0.984222	0.984614	0.984997	0.985371	0.985738
2.2	0.986097	0.986447	0.986791	0.987126	0.987455	0.987776	0.988089	0.988396	0.988696	0.988989
2.3	0.989276	0.989556	0.989830	0.990097	0.990358	0.990613	0.990863	0.991106	0.991344	0.991576
2.4	0.991802	0.992024	0.992240	0.992451	0.992656	0.992857	0.993053	0.993244	0.993431	0.993613
2.5	0.993790	0.993963	0.994132	0.994297	0.994457	0.994614	0.994766	0.994915	0.995060	0.995201
2.6	0.995339	0.995473	0.995604	0.995731	0.995855	0.995975	0.996093	0.996207	0.996319	0.996427
2.7	0.996533	0.996636	0.996736	0.996833	0.996928	0.997020	0.997110	0.997197	0.997282	0.997365
2.8	0.997445	0.997523	0.997599	0.997673	0.997744	0.997814	0.997882	0.997948	0.998012	0.998074
2.9	0.998134	0.998193	0.998250	0.998305	0.998359	0.998411	0.998462	0.998511	0.998559	0.998605
3.0	0.998650	0.998694	0.998736	0.998777	0.998817	0.998856	0.998893	0.998930	0.998965	0.998999
3.1	0.999032	0.999065	0.999096	0.999126	0.999155	0.999184	0.999211	0.999238	0.999264	0.999289
3.2	0.999313	0.999336	0.999359	0.999381	0.999402	0.999423	0.999443	0.999462	0.999481	0.999499
3.3	0.999517	0.999533	0.999550	0.999566	0.999581	0.999596	0.999610	0.999624	0.999638	0.999650
3.4	0.999663	0.999675	0.999687	0.999698	0.999709	0.999720	0.999730	0.999740	0.999749	0.999758
3.5	0.999767	0.999776	0.999784	0.999792	0.999800	0.999807	0.999815	0.999821	0.999828	0.999835
3.6	0.999841	0.999847	0.999853	0.999858	0.999864	0.999869	0.999874	0.999879	0.999883	0.999888
3.7	0.999892	0.999896	0.999900	0.999904	0.999908	0.999912	0.999915	0.999918	0.999922	0.999925
3.8	0.999928	0.999931	0.999933	0.999936	0.999938	0.999941	0.999943	0.999946	0.999948	0.999950
3.9	0.999952	0.999954	0.999956	0.999958	0.999959	0.999961	0.999963	0.999964	0.999966	0.999967

What may be on the final exam?

- Probability Multiplication, Combinatorics
- Bayes Theorem
- Discrete & Continuous Random Variables
- Joint Probability Distributions, Covariation/Correlations
- Sampling distributions and parameter point estimation
- Confidence Intervals
- Hypothesis testing for one and two samples
- Other topics
- Look at Homework 1-5 for examples of problems

One-sample hypothesis testing

3. (8 points) The college bookstore tells prospective students that the average cost of its textbooks is \$52 with a standard deviation of \$4.50. A group of statistics students think that the average cost is actually higher. In order to test bookstore's claim against this alternative hypothesis, the students bought a random sample of 100 books. The mean price of this sample was \$52.80. Perform the hypothesis test at the 5% level of significance and state your decision.

What type of hypothesis should I apply?

A. Two-sided: $\mu_1 \neq \mu_0$

B. One-sided: $\mu_1 > \mu_0$

C. One-sided: $\mu_1 < \mu_0$

D. Three-sided

E. I have no idea

Get your i-clickers

3. (8 points) The college bookstore tells prospective students that the average cost of its textbooks is \$52 with a standard deviation of \$4.50. A group of statistics students think that the average cost is **actually higher**. In order to test bookstore's claim against this alternative hypothesis, the students bought a random sample of 100 books. The mean price of this sample was \$52.80. Perform the hypothesis test at the 5% level of significance and state your decision.

The standard deviation of \bar{x} in this sample is:

A. \$4.50

B. \$45

C. \$0.45

D. I have no idea

Get your i-clickers

3. (8 points) The college bookstore tells prospective students that the average cost of its textbooks is \$52 with a standard deviation of \$4.50. A group of statistics students think that the average cost is **actually higher**. In order to test bookstore's claim against this alternative hypothesis, the students bought a random sample of 100 books. The mean price of this sample was \$52.80. Perform the hypothesis test at the 5% level of significance and state your decision.

3. (8 points) The college bookstore tells prospective students that the average cost of its textbooks is \$52 with a standard deviation of \$4.50. A group of statistics students think that the average cost is actually higher. In order to test bookstore's claim against this alternative hypothesis, the students bought a random sample of 100 books. The mean price of this sample was \$52.80. Perform the hypothesis test at the 5% level of significance and state your decision.

Answer: Hypothesis: $\begin{cases} H_0 : \mu = 52 \\ H_1 : \mu > 52 \end{cases}$. The critical z-value can be obtained from $z^* = \frac{52.8 - 52}{4.5 / 10} = 1.78$. Since $z^* > z_\alpha = 1.65$, this test statistic lies in the rejection region for H_0 . Thus null hypothesis H_0 will be rejected and alternative hypothesis H_1 is accepted.

Two-sample hypothesis

Mating Calls. In a study of mating calls in the gray treefrogs *Hyla chrysoscelis* and *Hyla versicolor*, Gerhart (1994) reports that in a location in Louisiana the following data on the length of male advertisement calls have been collected:

	Sample size	Average duration	SD of duration	Duration range
<i>Hyla chrysoscelis</i>	43	0.65	0.18	0.36–1.27
<i>Hyla versicolor</i>	12	0.54	0.14	0.36–0.75

The two species cannot be distinguished by external morphology, but *H. chrysoscelis* are diploids while *H. versicolor* are tetraploids. The triploid crosses exhibit high mortality in larval stages, and if they attain sexual maturity, they are sterile. Females responding to the mating calls try to avoid mismatches.

Based on the data summaries provided, test whether the length of call is a discriminatory characteristic? Use $\alpha = 0.05$.

	Sample size	Average duration	SD of duration
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Based on the data summaries provided, test whether the length of call is a discriminatory characteristic? Use $\alpha = 0.05$.

1. Use two-sided hypothesis
2. $z_{\{\alpha/2\}}=1.96$
3. $Z=(0.65-0.54)/\text{sqrt}(0.18.^2/43+0.14.^2/12)=2.2516$
4. Since $Z > z_{\{\alpha/2\}}$ null hypothesis can be rejected

Confidence intervals

2. (6 points) The operations manager of a large production plant would like to estimate the mean amount of time a worker takes to assemble a new electronic component. Assume that the standard deviation of this assembly time is 3.6 minutes. After observing a sample of 100 workers assembling similar devices, the manager noticed that their average time was 16.2 minutes. Construct a 90% confidence interval for the population mean of the assembly time.

two-sided

What Z should I look up in the table?

- A. $\Phi(Z)=0.9$
- B. $\Phi(Z)=0.05$
- C. $\Phi(Z)=0.95$
- D. $\Phi(Z)=0.1$
- E. I have no idea

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2. (6 points) The operations manager of a large production plant would like to estimate the mean amount of time a worker takes to assemble a new electronic component. Assume that the standard deviation of this assembly time is 3.6 minutes. After observing a sample of 100 workers assembling similar devices, the manager noticed that their average time was 16.2 minutes. Construct a 90% confidence interval for the population mean of the assembly time.

What Z should I look up in the table?

- A. $\Phi(Z)=0.9$
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Get your i-clickers

2. (6 points) The operations manager of a large production plant would like to estimate the mean amount of time a worker takes to assemble a new electronic component. Assume that the standard deviation of this assembly time is 3.6 minutes. After observing a sample of 100 workers assembling similar devices, the manager noticed that their average time was 16.2 minutes. Construct a **90% confidence interval** for the population mean of the assembly time.

2. (6 points) The operations manager of a large production plant would like to estimate the mean amount of time a worker takes to assemble a new electronic component. Assume that the standard deviation of this assembly time is 3.6 minutes. After observing a sample of 100 workers assembling similar devices, the manager noticed that their average time was 16.2 minutes. Construct a **90% confidence interval** for the population mean of the assembly time.

Answer: Let μ denote the mean assembly time (in minutes). We want a 90% confidence interval for μ based on the following information: $n = 100$, $\bar{X} = 16.2$, $\alpha = 0.1$, $\sigma = 3.6$. Since σ is known, we can use normal distribution to calculate confidence interval:

$$\bar{X} \pm z_{\alpha/2} \frac{\sigma}{\sqrt{n}} = 16.2 \pm (1.65) \frac{3.6}{10} = [15.61, 16.79]$$

What is X in this problem?

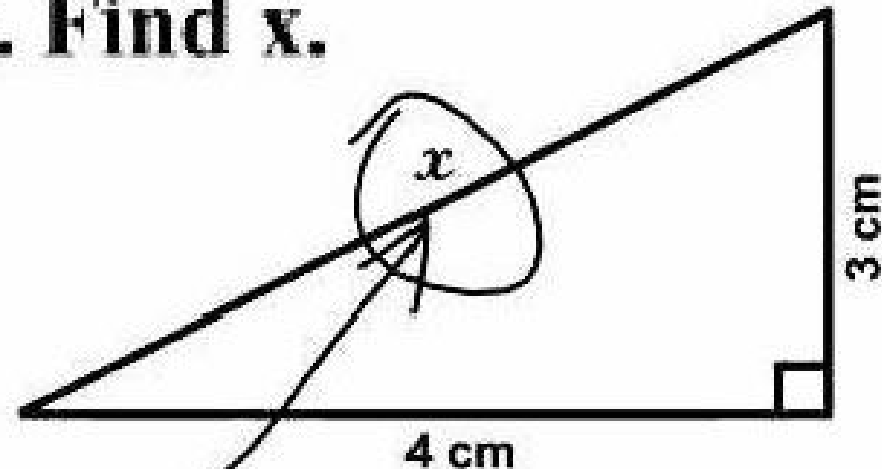
- **What is X?** Look for keywords:
 - Find the probability that....
 - What is the mean (or variance) of...
- **What are the parameters?**

Look for keywords:

- Given that...
- Assuming that...

- **Is X discrete or continuous?**

3. Find x.



Here it is

Discrete Probability Distributions

(8 points) You are doing a long series of experiments. Assume that each of your experiments has a probability of 0.02 of succeeding. Assume that your experiments are independent.

(A) (2 points) What is the probability that you first succeed on tenth experiment?

(B) (2 points) What is the probability that it requires more than five experiments for you to succeed?

(C) (2 points) What is the mean number of experiments needed to succeed once?

(D) (2 points) What is the probability that the second experiment that worked is the tenth one since you started?

2. (8 points, 2 points each) You are doing a long series of experiments. Assume that each of your experiments has a probability of 0.02 of succeeding. Assume that your experiments are independent.
- (a) What is the probability that you first succeed on tenth experiment?

$$P(X=10) = (1-0.02)^9 * 0.02 = 0.0167$$

- (b) What is the probability that it requires more than five experiments for you to succeed?

$$\begin{aligned} P(X > 5) &= 1 - P(X=1) - P(X=2) - P(X=3) - P(X=4) - P(X=5) \\ &= 1 - 0.98^0 * 0.02 - 0.98^1 * 0.02 - 0.98^2 * 0.02 - 0.98^3 * 0.02 - 0.98^4 * 0.02 = 0.9039 \\ \text{Easier solution: } P(X > 5) &= 0.98^5 = 0.9039 \end{aligned}$$

- (c) What is the mean number of experiments needed to succeed once?

$$\text{Since } X \text{ follows geometric distribution, the mean value of } X \text{ is } 1/0.02 = 50.$$

- (d) What is the probability that the second experiment that worked is the tenth one since you started
- $$\text{Probability} = 9 * 0.02 * 0.98^8 * 0.02 = 0.0031$$

Continuous Probability Distributions

(12 points) Time interval separating subsequent bus arrivals at a stop is an exponential random variable with mean 20 minutes. Steve and Andrew work at the same place and each will be late to work unless they board a bus on or before 8:40am. Steve comes to the bus stop exactly at 8am. Andrew also comes to the same bus stop but at a random time, uniformly distributed between 8am and 8:30am. Both of them take the first bus that arrives.

(a) (4 points) What is the probability that Steve will be late for work tomorrow?

(b) (4 points) What is the probability that Andrew will be late for work tomorrow?

(c) (4 points) What is the probability that Steve and Andrew will ride the same bus

(12 points) Time interval separating subsequent bus arrivals at a stop is an exponential random variable with mean 20 minutes. Steve and Andrew work at the same place and each will be late to work unless they board a bus on or before 8:40am. Steve comes to the bus stop exactly at 8am. Andrew also comes to the same bus stop but at a random time, uniformly distributed between 8am and 8:30am. Both of them take the first bus that arrives.

(a) **(4 points)** What is the probability that Steve will be late for work tomorrow?

$$\text{Answers: } P(\text{Steve late}) = 1 - P(T < 40) = 1 - \frac{1}{20} \int_0^{40} e^{-t/20} dt = e^{-2} = 0.1353$$

(b) **(4 points)** What is the probability that Andrew will be late for work tomorrow?

Answers:

$$P(\text{Andrew late}) = \int_0^{30} \frac{dx}{30} P(T \geq 40 | T > x) = \int_0^{30} \frac{dx}{30} e^{-(40-x)/20} = \frac{e^{-2}}{30} \int_0^{30} e^{x/20} dx = \frac{20e^{-2}}{30} (e^{30/20} - 1) = 0.3141$$

(c) **(4 points)** What is the probability that Steve and Andrew will ride the same bus?

Probability that Steve will not leave by the time x when Andrew comes is $\exp(-x/20)$.

It needs to be integrated over $\int_0^{30} dx/30 \exp(-x/20) =$

$$\text{Answers: } P(\text{Steve and Andrew meet}) = \int_0^{30} \frac{dx}{30} e^{-x/20} = \frac{20}{30} (1 - e^{-30/20}) = 0.5179$$

Credit: XKCD
comics

WHY ARE THERE SLAVES IN THE BIBLE

WHY DO TWINS HAVE DIFFERENT FINGERPRINTS
WHY ARE AMERICANS AFRAID OF DRAGONS

WHY IS HTTPS CROSSED OUT IN RED
WHY IS THERE A LINE THROUGH HTTPS
WHY IS THERE A RED LINE THROUGH HTTPS ON FACEBOOK
WHY IS HTTPS IMPORTANT

QUESTIONS

FOUND IN GOOGLE AUTOCOMLETE



WHY ARE THERE WEEKS
WHY DO I FEEL DIZZY

WHY AREN'T ECONOMISTS RICH

WHY ARE THERE SO MANY CROWS IN ROCHESTER, MN
WHY IS THERE PHLEGM

WHY DO AMERICANS CALL IT SOCCER

WHY IS PSYCHIC WEAK TO BUG

WHY ARE MY EARS RINGING

WHY DO CHILDREN GET CANCER

WHY ARE THERE SO MANY AVENGERS

WHY IS POSEIDON ANGRY WITH ODYSSEUS

WHY ARE THE AVENGERS FIGHTING THE X MEN

WHY IS THERE ICE IN SPACE

WHY ARE THERE ANTS IN MY LAPTOP

WHY IS EARTH TILTED

WHY ARE THERE GHOSTS

WHY IS THERE AN OWL IN MY BACKYARD

WHY IS SPACE BLACK

WHY ARE THERE GHOSTS

WHY IS THERE AN OWL OUTSIDE MY WINDOW

WHY IS OUTER SPACE SO COLD

WHY ARE THERE GHOSTS

WHY IS THERE AN OWL ON THE DOLLAR BILL

WHY ARE THERE PYRAMIDS ON THE MOON

WHY ARE THERE GHOSTS

WHY DO OWLS ATTACK PEOPLE

WHY IS NASA SHUTTING DOWN

WHY ARE THERE GHOSTS

WHY ARE AK 47s SO EXPENSIVE

WHY ARE THERE MALE AND FEMALE BIKES

WHY ARE THERE GHOSTS

WHY ARE THERE HELICOPTERS CIRCLING MY HOUSE

WHY ARE THERE TINY SPIDERS IN MY HOUSE

WHY ARE THERE GHOSTS

WHY ARE THERE GODS

WHY DO SPIDERS COME INSIDE

WHY ARE THERE GHOSTS

WHY ARE THERE TWO SPOCKS

WHY ARE THERE HUGE SPIDERS IN MY HOUSE

WHY ARE THERE GHOSTS

WHY IS LIFE SO BORING

WHY ARE THERE LOTS OF SPIDERS IN MY HOUSE

WHY ARE THERE GHOSTS

WHY ARE CIGARETTES LEGAL

WHY ARE THERE SPIDERS IN MY ROOM

WHY ARE THERE GHOSTS

WHY ARE THERE DUCKS IN MY POOL

WHY ARE THERE SO MANY SPIDERS IN MY ROOM

WHY ARE THERE GHOSTS

WHY IS JESUS WHITE

WHY DO WHALES JUMP

WHY ARE WITCHES GREEN

WHY ARE THERE MIRRORS ABOVE BEDS

WHY DO I SAY UH

WHY IS SEA SALT BETTER

WHY ARE THERE TREES IN THE MIDDLE OF FIELDS

WHY IS THERE NOT A POKEMON MMO

WHY IS THERE LAUGHING IN TV SHOWS

WHY ARE THERE DOORS ON THE FREEWAY

WHY ARE THERE SO MANY SVCHOST.EXE RUNNING

WHY AREN'T THERE ANY COUNTRIES IN ANTARCTICA

WHY ARE THERE SCARY SOUNDS IN MINECRAFT

WHY IS THERE KICKING IN MY STOMACH

WHY ARE THERE TWO SLASHES AFTER HTTP

WHY ARE THERE CELEBRITIES

WHY DO SNAKES EXIST

WHY DO OYSTERS HAVE PEARLS

WHY ARE DUCKS CALLED DUCKS

WHY DO THEY CALL IT THE CLAP

WHY ARE KYLE AND CARTMAN FRIENDS

WHY IS THERE AN ARROW ON AANG'S HEAD

WHY ARE TEXT MESSAGES BLUE

WHY ARE THERE MUSTACHES ON CLOTHES

WHY ARE THERE MUSTACHES ON CARS

WHY ARE THERE MUSTACHES EVERYWHERE

WHY DO IGUANAS DIE

DINOSAUR GHOSTS

WHY ARE THERE FEMALE MR NIMES

WHY ARE THERE BRIDESMAIDS

WHY DO DYING PEOPLE REACH UP

WHY AREN'T THERE VARICOSE ARTERIES

WHY ARE OLD KUNGONS DIFFERENT

WHY ARE THERE SQUIRRELS

WHY IS THERE HELL IF GOD FORGIVES

WHY IS THERE NO GPS IN LAPTOPS

WHY DO KNEES CLICK

WHY AREN'T THERE E GRADES

WHY IS ISOLATION BAD

WHY IS THERE HELL IF GOD FORGIVES

WHY IS THERE HELL IF GOD FORGIVES

WHY IS THERE HELL IF GOD FORGIVES

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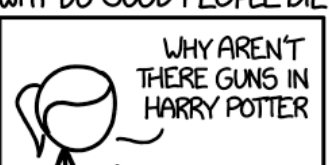
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WHY IS SEX SO IMPORTANT



WHY ARE DOGS AFRAID OF FIREWORKS
WHY IS THERE NO KING IN ENGLAND

WHY ARE ULTRASOUNDS IMPORTANT
WHY ARE ULTRASOUND MACHINES EXPENSIVE
WHY IS STEALING WRONG
WHY AREN'T THERE ANY FOREIGN MILITARY BASES IN AMERICA