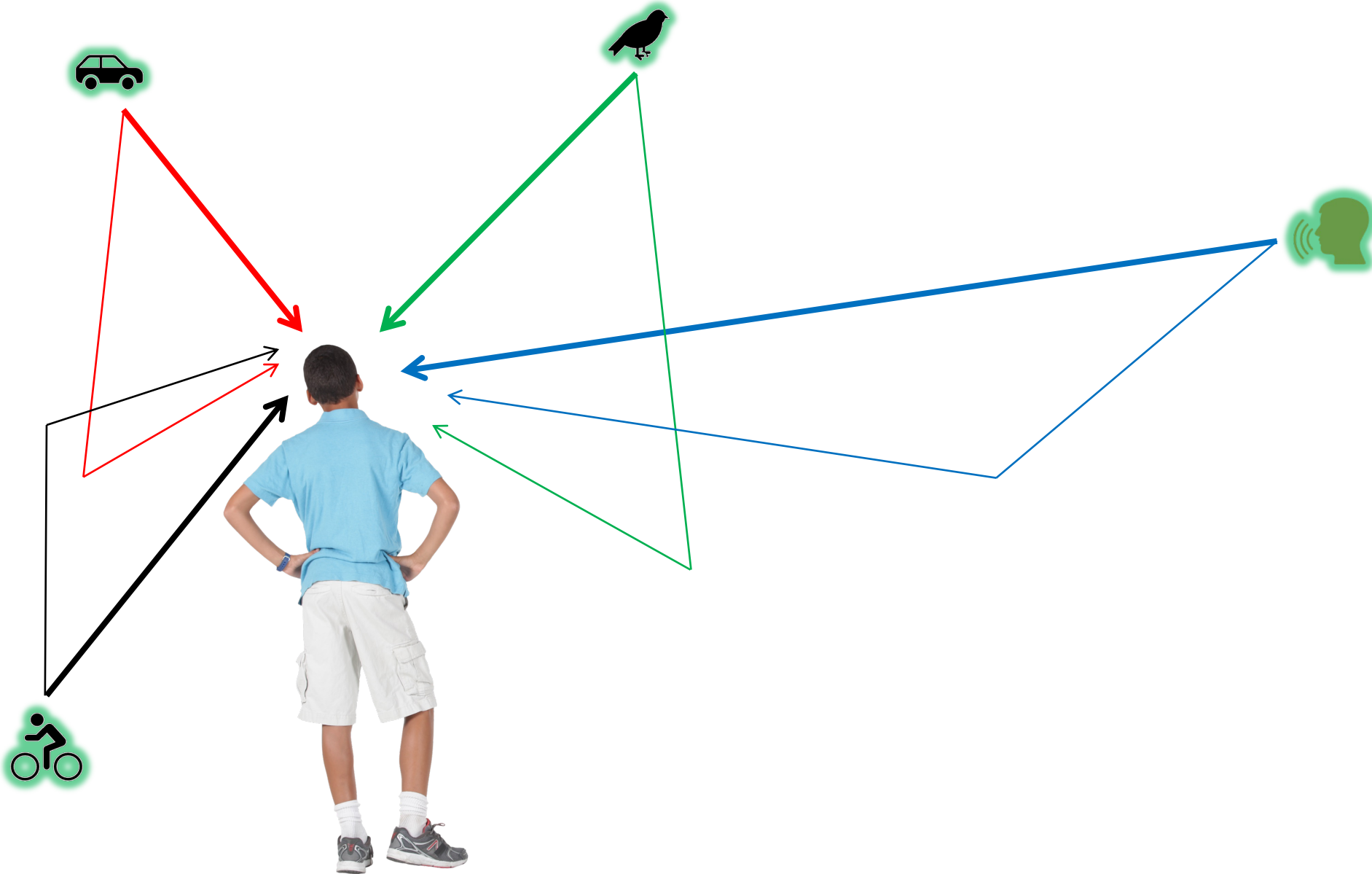


Source separation



Source separation

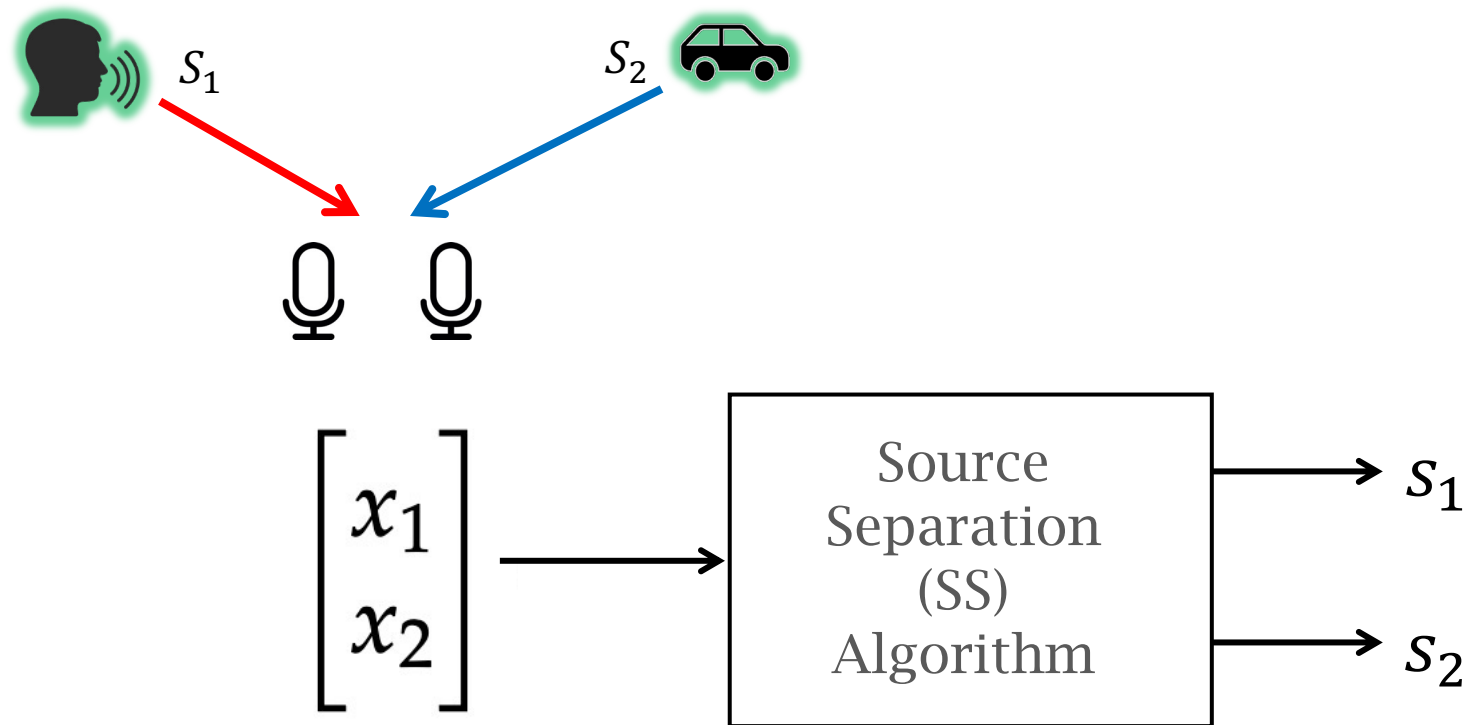


Source separation



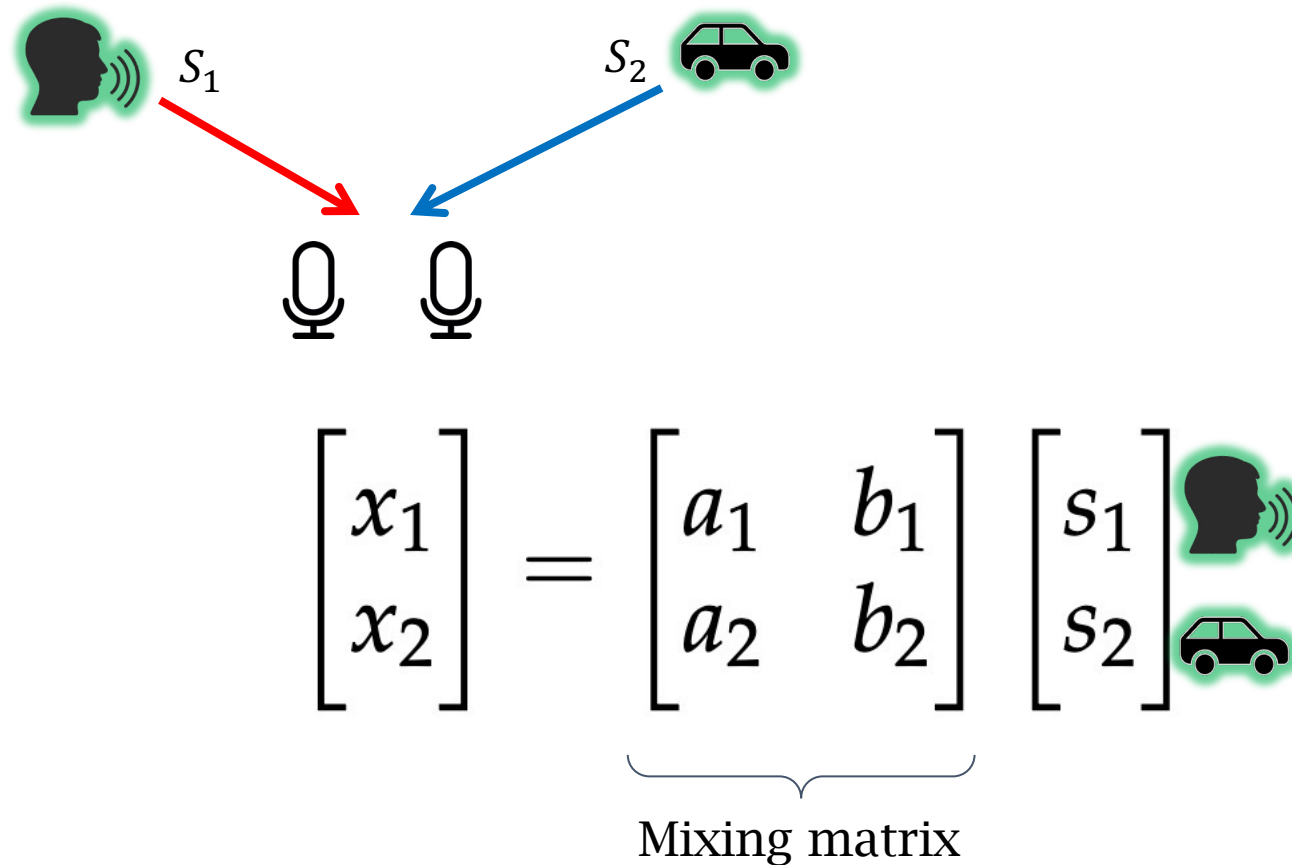
Source separation preliminaries

Source separation: The general problem statement



Source separation preliminaries

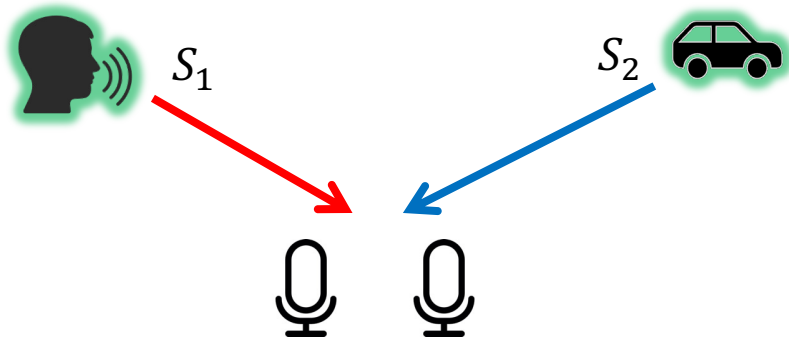
Source separation: The general problem statement



Unknown mixing matrix, unknown source signals \rightarrow heavily under-determined

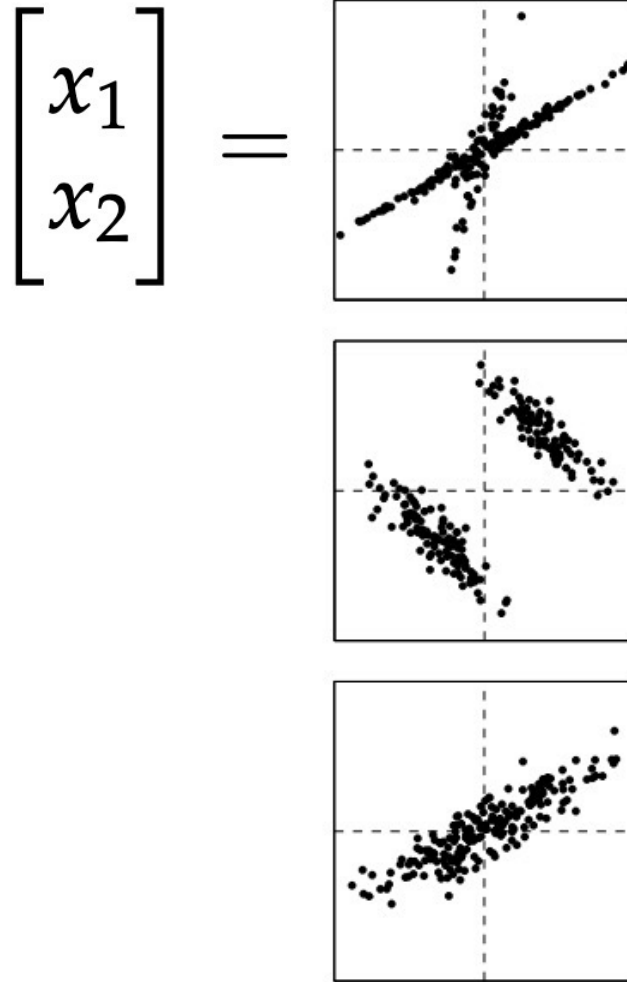
Source separation preliminaries

Source separation: The general problem statement



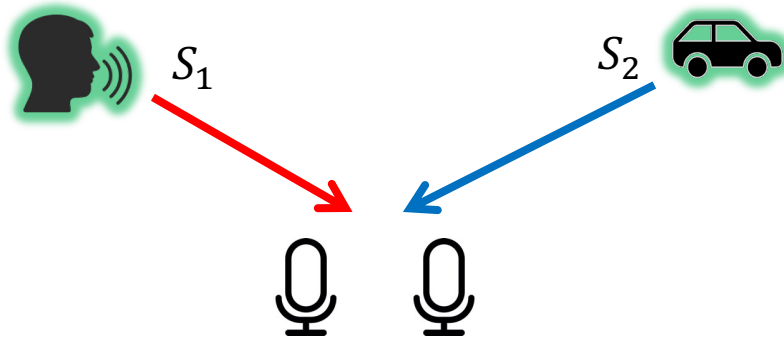
$$\begin{bmatrix} x_1 \\ x_2 \end{bmatrix} = \begin{bmatrix} a_1 & b_1 \\ a_2 & b_2 \end{bmatrix} \begin{bmatrix} s_1 \\ s_2 \end{bmatrix}$$

Mixing matrix



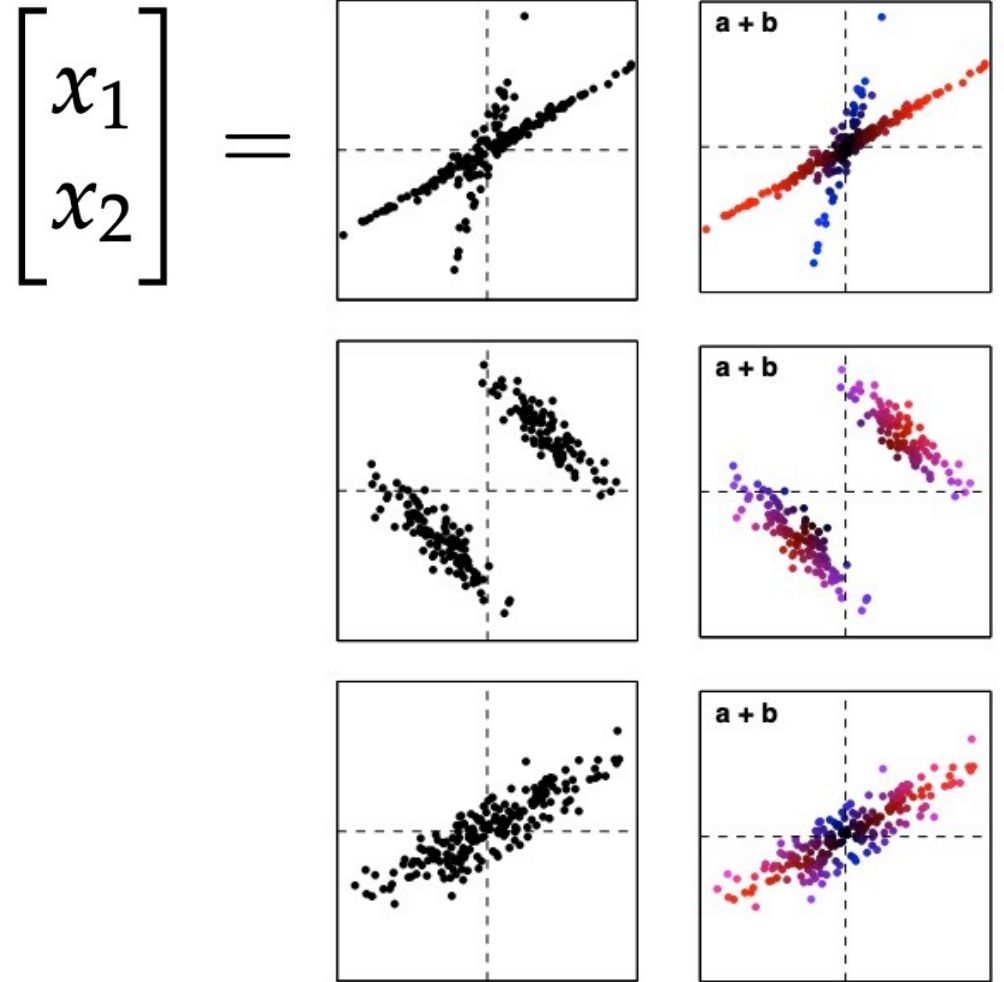
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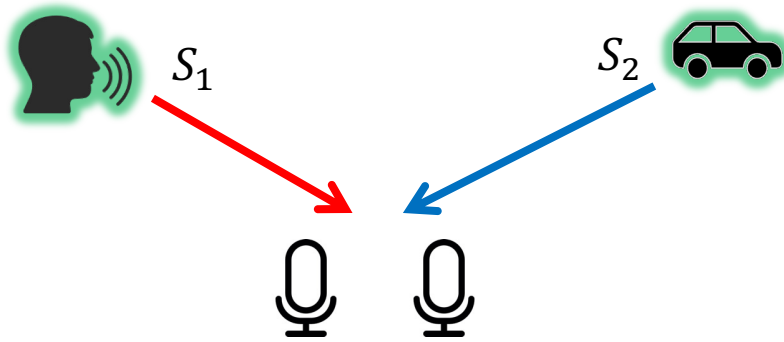
Mixing matrix



Hard to separate the sources even visually

When can we solve SS?

Let's make some simplifications: Mixing matrix is known based on **Angle of Arrival (AOA)**



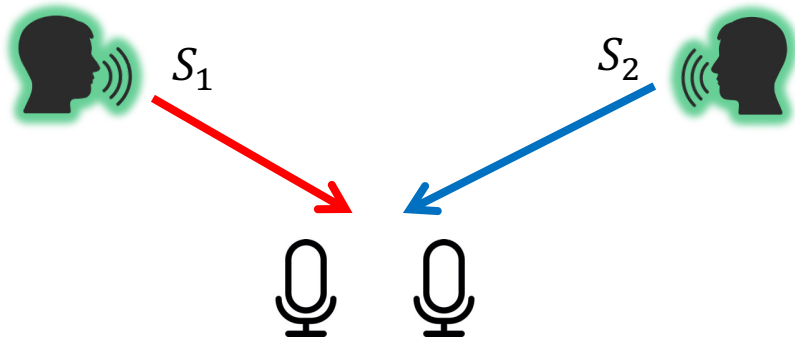
- What is angle of arrival (AoA)? How do you quantify it?
- Relation between AoA and FFT
- How do you get AoA? From camera or from audio itself?
- How to solve $X = A S + N$ even when A is known

$$\begin{bmatrix} x_1 \\ x_2 \end{bmatrix} = \underbrace{\begin{bmatrix} | & | \\ \vec{a}_{\theta_1} & \vec{a}_{\theta_2} \\ | & | \end{bmatrix}}_{\text{AoA matrix } A} \begin{bmatrix} s_1 \\ s_2 \end{bmatrix}$$

$$X = A.S + N$$

Source = Speech

But what if AoA unknown? **It's hard to solve for S ... but what if S is speech signals?**



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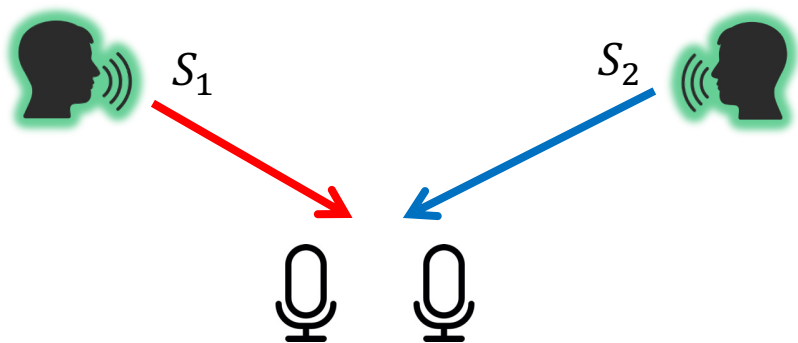
AoA matrix A

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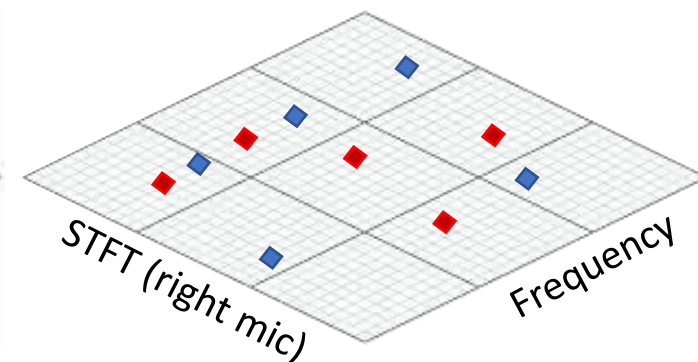
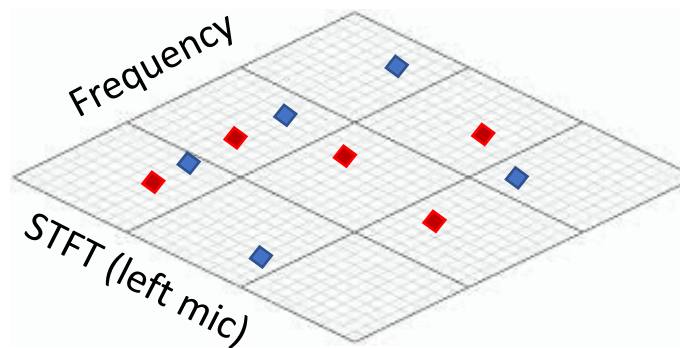
When the source signal is speech, exploit TF-disjointness



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AoA matrix A

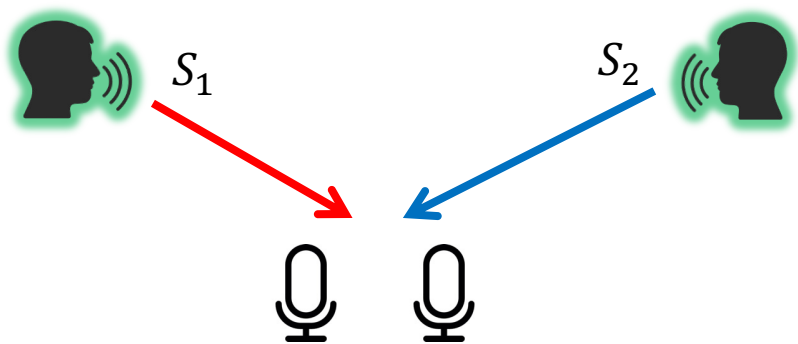
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Source = Speech

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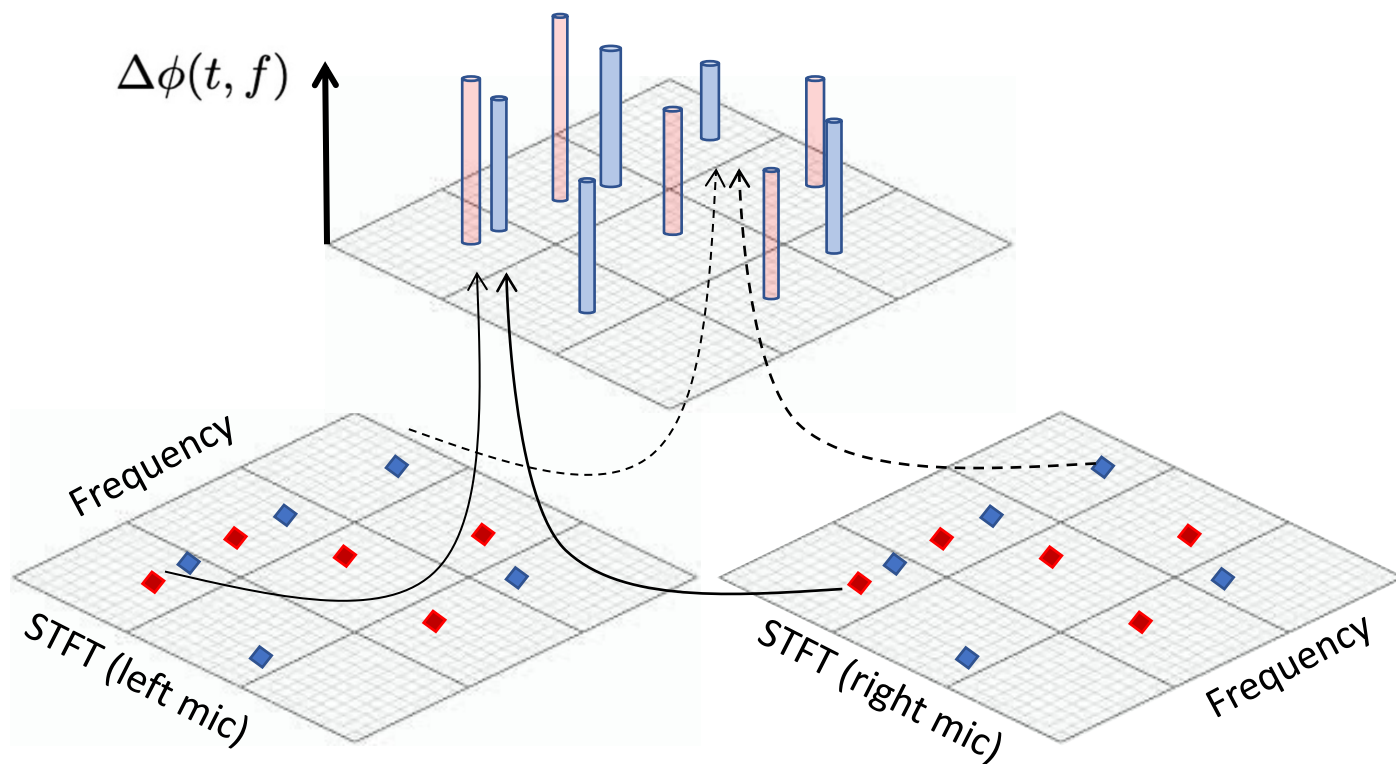
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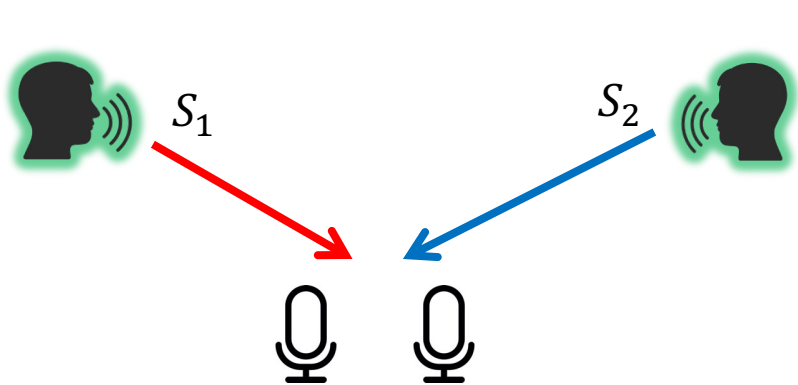
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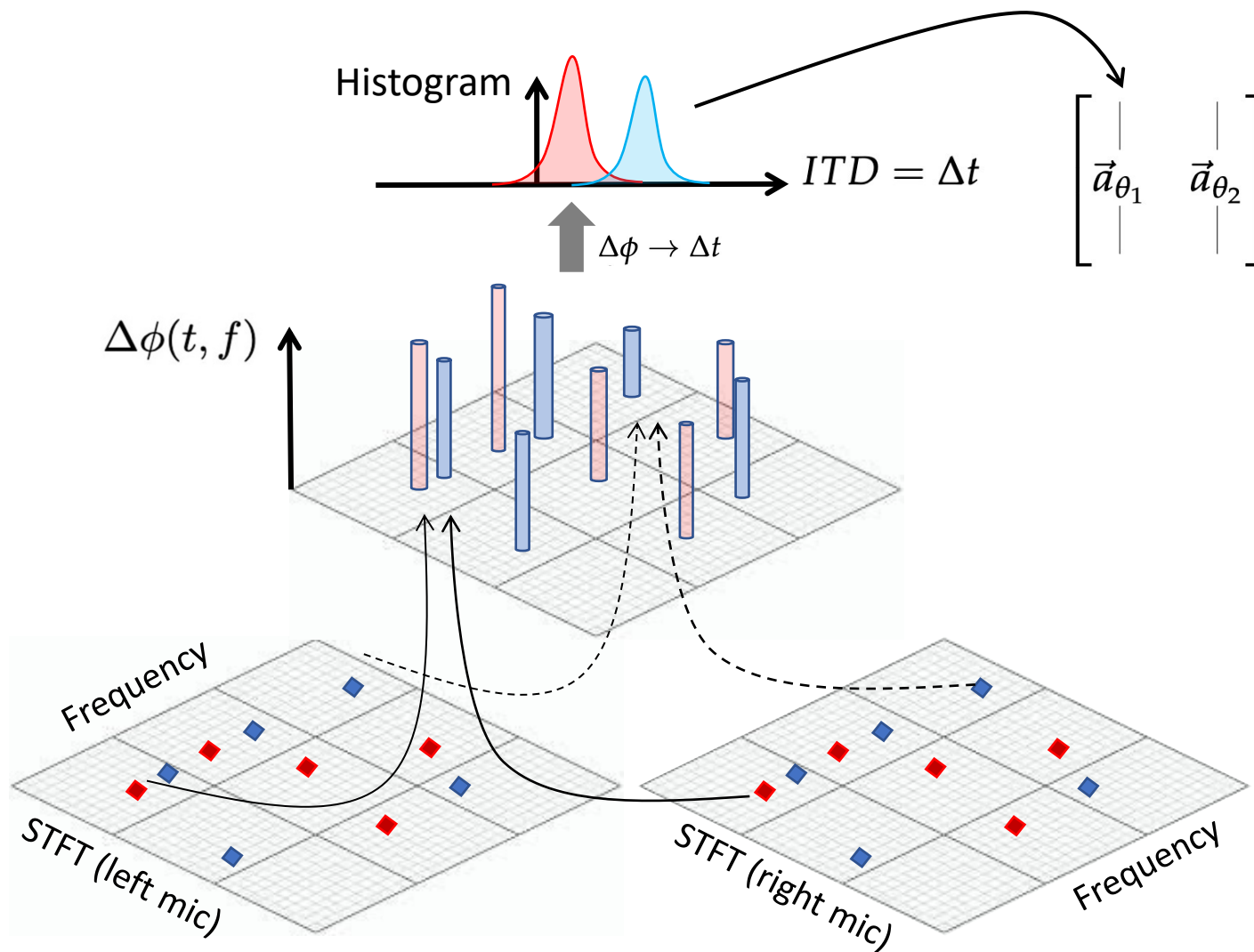
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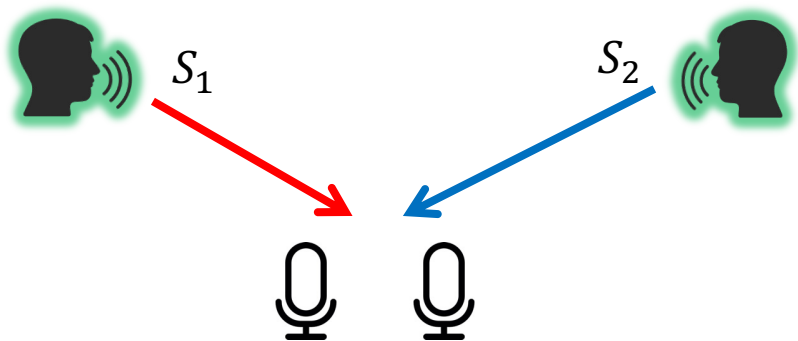
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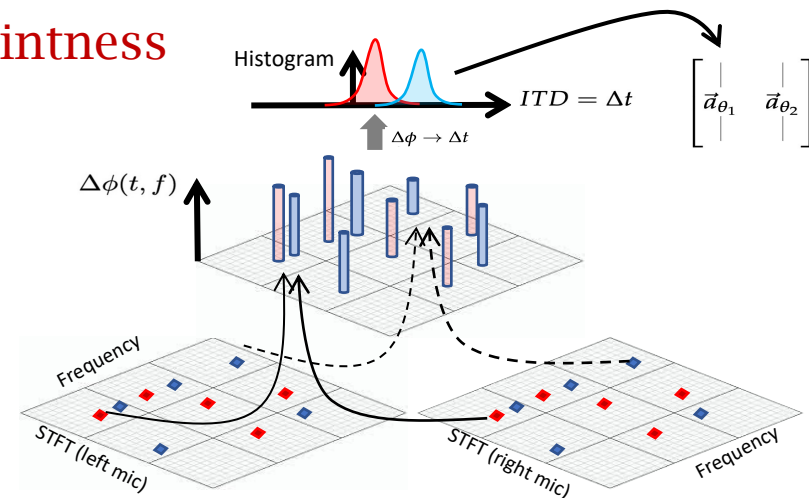
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AoA matrix A

$$X = A.S + N$$



DUET Algorithm Steps:

- 1.
- 2.
- 3.
- 4.
- 5.

